



Experimental Results for a Nonlinear Equation Using Improved Newton-Raphson Estimation Method

Mohammed RASHEED^{a, *}, Suha SHIHAB^b, Taha RASHID^c, Yaseen Hadi Ali^d

^aApplied Science Department, University of Technology, Baghdad, Iraq, e-mail: rasheed.mohammed40@yahoo.com, 10606@uotechnology.edu.iq.

^bApplied Science Department, University of Technology, Baghdad, Iraq, e-mail: alrawy1978@yahoo.com, 100031@uotechnology.edu.iq.

^cComputer and Microelectronics System, Faculty of Engineering, University Technology Malaysia (UTM), Skudai 81310, Johor Bahru, Malaysia, e-mail: tsiham95@gmail.com, taha1988@graduate.utm.my.

^dElectronic and Telecommunications Engineering, Faculty of Engineering, University Technology Malaysia (UTM), Skudai 81310, Johor Bahru, Malaysia, e-mail: hadi1995@graduate.utm.my.

ARTICLE INFO

Article history:

Received: 21 /01/2020

Revised form: 21 /02/2021

Accepted : 23 /03/2021

Available online: 24 /03/2021

Keywords:

Predictor-Corrector type algorithm;
 Newton's algorithm; modelling;
 voltage; initial value

ABSTRACT

In this paper, two algorithms for solving the nonlinear equation of the solar cell within single diode model are proposed. These algorithms are plays an important and significant rule in the evaluation of this equation. The solution is examined with a various values of load resistance (1, 5) Ω at room temperature. The nonlinear equation of a solar cell is derived from the equivalent circuit of this cell. The obtained results reveal that the propose algorithm is appropriate one for solving such equations with the aid of Matlab language.

MSC. 41A25; 41A35; 41A36

DOI : <https://doi.org/10.29304/jqcm.2021.13.1.782>

1. Introduction

Most of the numerical methods used to solve nonlinear equations are a kind of iterative methods. Therefore, we need the initial value of the root from which we can generate a sequential of approximate values that are another value of the root of the equation and approach it as the values of the approach speed of the root increase, which depends mainly on correct choice of starting point. There are many ways to solve nonlinear equations that are available in all other sciences such as engineering, science, medicine and mathematics [1-20]. The cheapest and least expensive semiconductor element is silicon, which is the second element in the earth's crust. The monopoly of

*Corresponding author: Mohammed RASHEED

Email addresses: rasheed.mohammed40@yahoo.com , 10606@uotechnology.edu.iq

Communicated by: *Dr. Rana Jumaa Surayh aljanabi*

nanomaterials for the unusual optical, electrical, and chemical properties of conventional granular materials has greatly increased their chances of being employed in the production of an advanced and distinctive generation of solar cells known as the third generation [21-96].

The aim of this article is to investigate a new iterative algorithm; predictor-corrector type technique (A1) in order to solve nonlinear equation of a PV cell. The following steps describe the next sections: section two and three characterizing the model of a PV cell and establishing the zeros finding of Newton Raphson algorithm respectively; while in section four predictor-corrector type algorithm has been depicted; section five and six; results, discussion and conclusions respectively.

2. PV Model Design (An Electrical Circuit)

Figure 1 illustrates PV cell an equivalent circuit (single diode model)

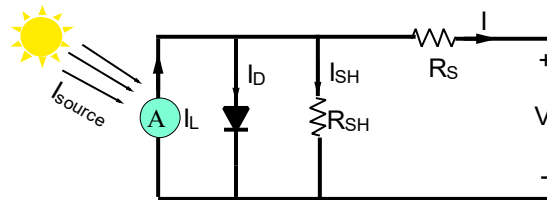


Fig. 1 - PV cell electrical equivalent circuit.

KCL-Kirchhoff's current law have been applied on Figure 1; a final equation of the PV cell current is extracted according to this equivalent as follows

$$I = I_{ph} - I_D \quad (1)$$

$$I_D = I_0 (e^{-V_{pv}/nV_T} - 1) \quad (2)$$

$$I = I_{ph} - I_0 \times (e^{-V_{pv}/nV_T} - 1) \quad (3)$$

where:

k , $V_T = kT/q = 26$ mV, q , T , I_0 , $1 < n < 2$ and I_{ph} : Boltzmann constant = 1.38×10^{-23} J/K, thermic voltage, the electron charge = 1.6×10^{-19} C, temperature (K), reverse saturation current, the recombination factor and the photocurrent (A) respectively.

$$I_{ph} = I_{source} \quad (4)$$

$$I_D = I_s * (e^{V_D/nV_T} - 1) \quad (5)$$

Subs. Eq. 4 in Eq. 5 yield

$$(I_{source}) - 10^{-12} \left(e^{\frac{-V}{1.2 \times 0.026}} - 1 \right) = \frac{V}{R} \quad (6)$$

where I_s reverse saturation current = 10^{-12} A. In parallel, $V_D = V = V_{pv}$

Based on the first derivative of Eq. 6; V can be determined numerically.

3. Newton's Method

- [1] The following algorithm suggestion for solving Eq. 6 by using NRM
- [2] $x_0 = 1$, input initial approximate solution.
- [3] x_{n+1} the output solution
- [4] Step 1- Set $x = 0$
- [5] Step 2- while $i \leq x_0$

[6] Step 3- Determine $x_{n+1} = x_n - \frac{f(x_n)}{f'(x_n)}$ for $n = 0, 1, 2, \dots$ (7)

[7] Step 4- if $|x_i - x_{i-1}| < \epsilon$; then x_{n+1} and stop.

[8] Step 5- Set $n = n + 1$; $i = i + 1$ and return to step 2.

[9] Step 6- OUTPUT

4. Predictor - Corrector Type (A1)

To compare the different numerical methods of iterations, methods 1 NRM has been used against the proposed method 2 Predictor-Corrector Type (A1). In addition; Eq. 6. has been solved to demonstrate the performance of the new method, the results are examined using some iteration.

Using the predictor-corrector type technique, we suggest the following two-step method, which is acquired by combining the Newton's method to obtain algorithm 1.

For a given H_0 , compute the approximate solution H_{n+1} by the iterative scheme

$$H_{n+1} = H_n - \frac{f(H_n)}{f'(H_n)} \tag{8}$$

$$H_{n+1} = H_n - \frac{6 \times f(H_n)}{f(H_n) + 4 \times f\left(\frac{H_n + H_{n+1}^*}{2}\right) + f(H_{n+1}^*)}, n = 0, 1, 2, 3, \dots \tag{9}$$

where x_0 is an initial value.

By assuming that $\epsilon = 10^{-9}$ as a tolerance; the following criteria is used for estimating the zero $\sigma = |H_{n+1} - H_n| < \epsilon$, $|f(H_n)| < \epsilon$ (10)

5. Results and Discussion

The roots of Eq. 6 (non-linear equation) are obtained by means of two techniques NRM and AHM extracted by Eqns. 7 and 9 with predict guess v_0 . The approximate solutions produced by the two methods. Five various numerical experiments are used using equation 6 which are based on the Resistance values (load resistance) which is varies between 1 to 5 ohm as illustrated in the Tables 1-5 and Figs 2-6. The results show that A1 technique need 7 iterations while NRM need 9 iterations respectively in order to reach to the convergence which proves that A1 is faster than the other method.

Table 1 - Total number of iterations for PV cell test case-two iteration methods NRM and A1.

Iterations	V_{pv} -NRM	I_{pv} - NRM	P_{pv} -NRM	V_{pv} -A1	I_{pv} -A1	P_{pv} -A1
1	1	1	1	0.956353318	0.956353318	0.914611669
2	0.971416861	0.971416861	0.943650719	0.935681181	0.935681181	0.875499273
3	0.946732606	0.946732606	0.896302627	0.924882295	0.924882295	0.85540726
4	0.929865706	0.929865706	0.864650231	0.922517684	0.922517684	0.851038878
5	0.923247893	0.923247893	0.852386673	0.922423278	0.922423278	0.850864704
6	0.922434	0.922434	0.850884484	0.922423135	0.922423135	0.850864439
7	0.922423136	0.922423136	0.850864443	0.922423135	0.922423135	0.850864439
8	0.922423135	0.922423135	0.850864439			
9	0.922423135	0.922423135	0.850864439			

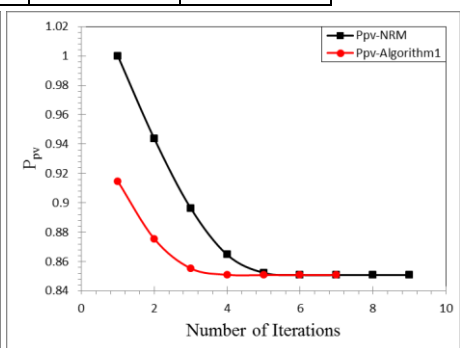
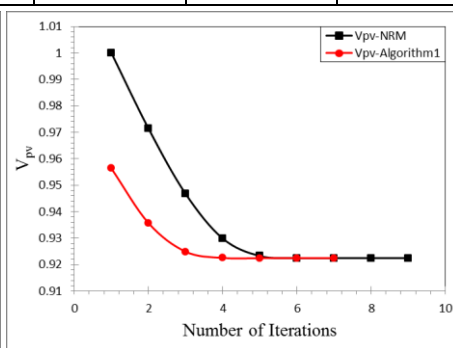
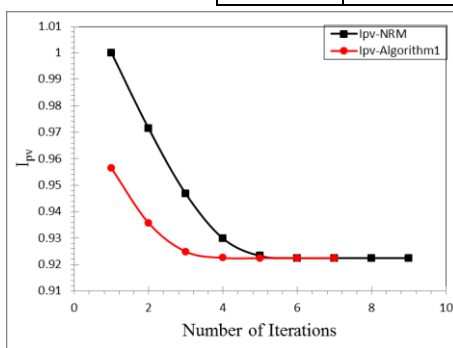


Fig. 2 – Measured PV parameters for the NRM and A1 algorithms.

Table 2 - Total number of iterations for PV cell test case-two iteration methods NRM and A1.

Iterations	V _{pv} -NRM	I _{pv} -NRM	P _{pv} -NRM	V _{pv} -A1	I _{pv} -A1	P _{pv} -A1
1	1	0.5	0.5	0.955521013	0.477760507	0.456510203
2	0.971030472	0.485515236	0.471450089	0.93345809	0.466729045	0.435672003
3	0.945421967	0.472710983	0.446911348	0.920709796	0.460354898	0.423853264
4	0.926834477	0.463417238	0.429511073	0.917245217	0.458622609	0.420669394
5	0.918438746	0.459219373	0.421764865	0.917036095	0.458518047	0.4204776
6	0.917066885	0.458533442	0.420505836	0.917035382	0.458517691	0.420476946
7	0.917035399	0.458517699	0.420476961	0.917035382	0.458517691	0.420476946
8	0.917035382	0.458517691	0.420476946			
9	0.917035382	0.458517691	0.420476946			

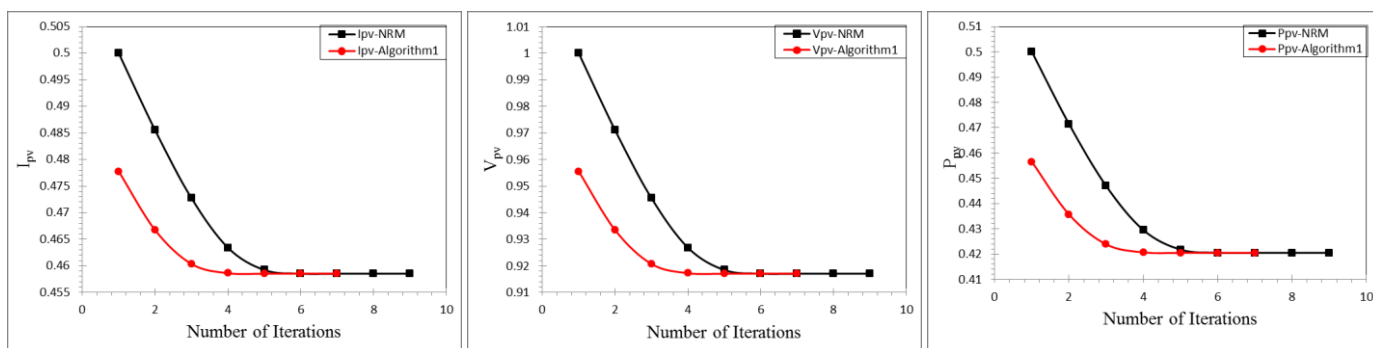


Fig. 3 – Measured PV parameters for the NRM and A1 algorithms.

Table 3 - Total number of iterations for PV cell test case-two iteration methods NRM and A1.

Iterations	V _{pv} -NRM	I _{pv} -NRM	P _{pv} -NRM	V _{pv} -A1	I _{pv} -A1	P _{pv} -A1
1	1	0.333333333	0.333333333	0.954680538	0.318226846	0.303804977
2	0.970643792	0.323547931	0.31404979	0.931137845	0.310379282	0.289005896
3	0.944084232	0.314694744	0.297098346	0.916052182	0.305350727	0.2797172
4	0.923594243	0.307864748	0.284342109	0.910893833	0.303631278	0.276575858
5	0.91287784	0.304292613	0.277781984	0.910407299	0.3034691	0.276280483
6	0.910501262	0.303500421	0.276337516	0.910403374	0.303467791	0.276278101
7	0.910403531	0.303467844	0.276278197	0.910403374	0.303467791	0.276278101
8	0.910403374	0.303467791	0.276278101			
9	0.910403374	0.303467791	0.276278101			

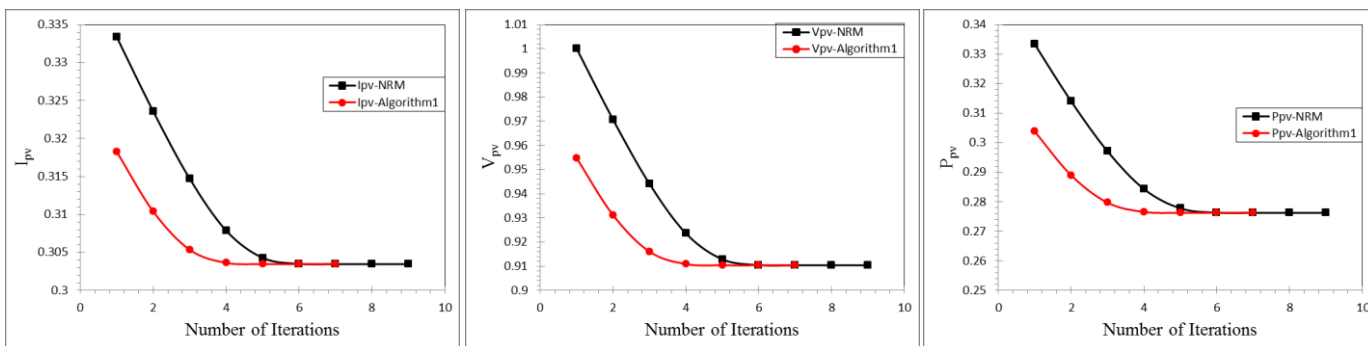


Fig. 4 – Measured PV parameters for the NRM and A1 algorithms.

Table 4 - Total number of iterations for PV cell test case-two iteration methods NRM and A1.

Iterations	V_{pv} -NRM	I_{pv} - NRM	P_{pv} -NRM	V_{pv} -A1	I_{pv} -A1	P_{pv} -A1
1	1	0.25	0.25	0.953831829	0.238457957	0.227448789
2	0.970256822	0.242564205	0.235349575	0.928714508	0.232178627	0.215627659
3	0.94271872	0.23567968	0.222179646	0.910814499	0.227703625	0.207395763
4	0.920123009	0.230030752	0.211656588	0.902979093	0.225744773	0.20384281
5	0.906346494	0.226586624	0.205365992	0.9017659	0.225441475	0.203295434
6	0.902077706	0.225519427	0.203436047	0.901740613	0.225435153	0.203284033
7	0.901742503	0.225435626	0.203284885	0.901740602	0.22543515	0.203284028
8	0.901740602	0.225435151	0.203284028	0.901740602	0.22543515	0.203284028
9	0.901740602	0.22543515	0.203284028			

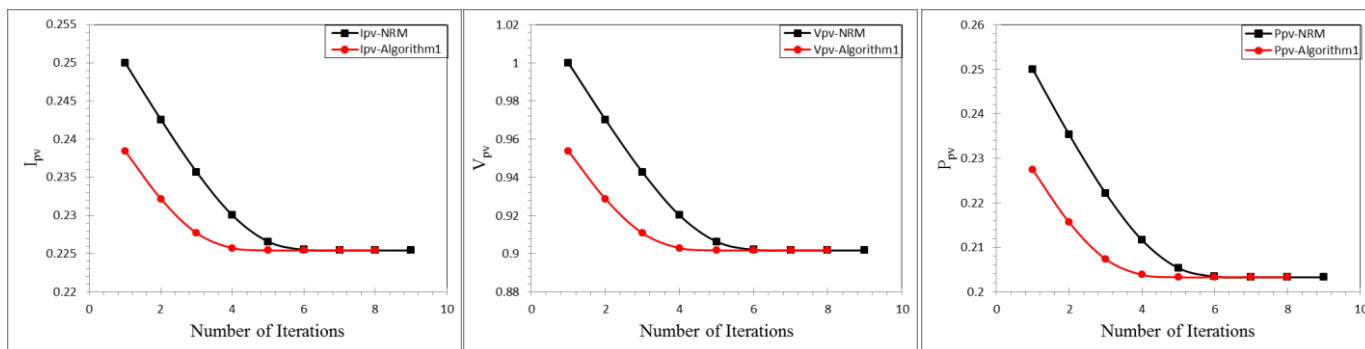


Fig. 5 – Measured PV parameters for the NRM and A1 algorithms.

Table 5 - Total number of iterations for PV cell test case-two iteration methods NRM and A1.

Iterations	V_{pv} -NRM	I_{pv} - NRM	P_{pv} -NRM	V_{pv} -A1	I_{pv} -A1	P_{pv} -A1
1	1	0.2	0.2	0.952974818	0.190594964	0.181632201
2	0.96986956	0.193973912	0.188129393	0.926181706	0.185236341	0.171562511
3	0.941324731	0.188264946	0.17721845	0.904877121	0.180975424	0.163760521
4	0.916395843	0.183279169	0.167956268	0.892668197	0.178533639	0.159371302
5	0.898535645	0.179707129	0.161473261	0.88930602	0.177861204	0.15817304
6	0.890477009	0.178095402	0.158589861	0.889093511	0.177818702	0.158097454
7	0.889125763	0.177825153	0.158108925	0.889092715	0.177818543	0.158097171
8	0.889092734	0.177818547	0.158097178	0.889092715	0.177818543	0.158097171
9	0.889092715	0.177818543	0.158097171			
10	0.889092715	0.177818543	0.158097171			

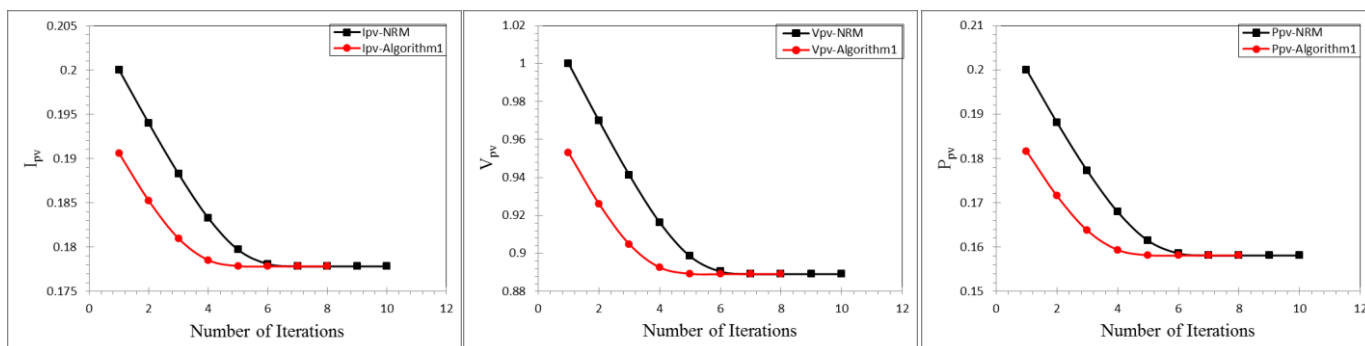


Fig. 6 – Measured PV parameters for the NRM and A1 algorithms.

6. Conclusion

Predictor-Corrector type and Newton's techniques were realized to obtain the numerical solution of the nonlinear equation of a solar cell. The two methods are examined by taking various values of the load resistance R and good results were achieved. The proposed method provided a very convenient and useful algorithm for the nonlinear equation. The results for the NRM were improved using Predictor-Corrector type to extract the roots of the single-diode equation within this algorithm by taking the initial value of x_0 .

References

- [1] M. M. Delphi and S. N. Shihab, "State Parameterization Basic Spline Functions for Trajectory Optimization", *Journal of Nature, Life and Applied Sciences*, vol. 3 (4) (2019), pp. 110-119.
- [2] S. Shihab and M. Delphi, "Direct Iterative Algorithm for Solving Optimal Control Problems Using B-Spline Polynomials", *Emirates Journal for Engineering Research*, vol. 24 (4) (2019), pp. 1-9.
- [3] M. Delphi and S. Shihab, "Modified Iterative Algorithm for Solving Optimal Control Problems", *Open Science Journal of Statistics and Application*, vol. 6 (2) (2019), pp. 20-27.
- [4] S. N. Shihab, A. A. Abdulrahman and M. N. Mohammed Ali, "Collocation Orthonormal Bernstein Polynomials Method for Solving Integral Equations", *Engineering and Technology Journal*, vol. 33 (8) (2015), pp. 1493-1502.
- [5] S. N. Shihab and T. N. Naif, "On the orthonormal Bernstein polynomial of order eight", *Open Science Journal of Mathematics and Application*, vol. 2 (2) (2014), pp. 15-19.
- [6] S. N. Shihab and A. A. Abdulrehman, "Solving Optimal Control Linear Systems by Using New Third kind Chebyshev Wavelets Operational Matrix of Derivative", *Baghdad Science Journal*, vol. 11 (2) (2014), pp. 229-234.
- [7] S. N. Shihab and A. A. Abdelrehman, "Some New Relationships Between the Derivatives of First and Second Chebyshev Wavelets", *International Journal of Engineering, Business and Enterprise Application*, (2012), pp. 64-68.
- [8] S. N. Shihab and A. A. Abdulrehman, "Numerical solution of calculus of variations by using the second Chebyshev wavelets", *Engineering and Technology Journal*, vol. 30 (18) (2012), pp. 3219-3229.
- [9] S. N. Shehab, H. A. Ali, H. M. Yaseen, "Least squares method for solving integral equations with multiple time lags", *Engineering & Technology Journal*, vol. 28 (10) (2010), pp. 1893-1899.
- [10] S. N. Al-Rawi, "On the Solution of Certain Fractional Integral Equations", *Journal of Kirkuk University–Scientific Studies*, vol. 1 (2) (2006).
- [11] S. N. Al-Rawi, R. K. Salih and A. A. Mohammed, "Numerical Solution of Nth Order Linear Delay Differential Equation Using Runge-Kutta Method", *Um - Salama Science Journal*, vol. 3 (1) (2006), pp. 140-146.
- [12] M. RASHEED, A. A. Abdulrahman, and S. Shihab, "The Effect of Set Partitioning in Hierarchical Trees with Wavelet Decomposition Levels Algorithm for Image Compression", *Electronics Science Technology and Application*, vol. 7 (3) (2020), pp. 40-46.
- [13] A. A. Abdulrahman, M. RASHEED and S. SHIHAB, "Various Techniques for De-noise Image, Electronics Science Technology and Application", vol. 7 (4) (2020), pp. 79-84.
- [14] A. A. Abdulrahman, M. RASHEED and S. SHIHAB, "Discrete Hermite Wavelet Filters with Prove Mathematical Aspects", *Journal of Southwest Jiaotong University*, vol. 55 (2) (2020), pp. 1-12.
- [15] A. A. Abdulrahman, M. RASHEED and S. SHIHAB, "Discrete Chebyshev Wavelet Transformation with Image Processing", *Journal of Southwest Jiaotong University*, vol. 55 (2) (2020), pp. 1-17.
- [16] M. S. Rasheed, H. S. Mahde, "Electronic Combination Lock Design Using Remote Control", *Journal of the College of Basic Education*, vol. 18 (75) (2012), pp. 265-280.
- [17] M. S. Rasheed and Balqis M. Diah, "Study of the effects of acidic solutions on the physical properties of polymeric materials superimposed", *Al-Mustansiriyah Journal of Science*, vol. 13 (49) (2002), pp. 6.
- [18] M. RASHEED and M. A. Sarhan, "Solve and Implement the main Equations of Photovoltaic Cell Parameters Using Visual Studio Program", *Insight-Mathematics*, vol. 1 (1) (2019), pp. 17-25.
- [19] M. Rasheed and M. A. Sarhan, "Characteristics of Solar Cell Outdoor Measurements Using Fuzzy Logic Method", *Insight-Mathematics*, vol. 1 (1) (2019), pp. 1-8.
- [20] M. RASHEED and M. A. Sarhan, "Measuring the Solar Cell Parameters Using Fuzzy Set Technique", *Insight-Electronic*, vol. 1 (1) (2019), pp. 1-9.
- [21] M. RASHEED, "Linear Programming for Solving Solar Cell Parameters", *Insight-Electronic*, vol. 1 (1) (2019), pp. 10-16.
- [22] M. RASHEED, "Investigation of Solar Cell Factors using Fuzzy Set Technique", *Insight-Electronic*, vol. 1 (1) (2019), pp. 17-23.
- [23] M. RASHEED and S. SHIHAB, "Analytical Modeling of Solar Cells", *Insight Electronics*, vol. 1 (2) (2019), pp. 1-9.
- [24] S. SHIHAB and M. RASHEED, "Modeling and Simulation of Solar Cell Mathematical Model Parameters Determination Based on Different Methods", *Insight Mathematics*, vol. 1 (1) (2019), pp. 1-16.
- [25] M. RASHEED and S. SHIHAB, "Parameters Estimation for Mathematical Model of Solar Cell", *Electronics Science Technology and Application*, vol. 6, (1) (2019), pp. 20-28.
- [26] M. Rasheed and S. Shihab, "Numerical Techniques for Solving Parameters of Solar Cell", *Applied Physics*, vol. 3 (1) (2020), pp. 16-27.
- [27] M. RASHEED and S. SHIHAB, "Modifications to Accelerate the Iterative Algorithm for the Single Diode Model of PV Model", *Iraqi Journal of Physics (IJP)*, vol. 18 (47) (2020), pp. 33-43.
- [28] M. S. Rasheed and S. Shihab, "Modelling and Parameter Extraction of PV Cell Using Single-Diode Model". *Advanced Energy Conversion Materials*, 1 (2) (2020), pp. 96-104. Available from: <http://ojs.wiserpub.com/index.php/AECM/article/view/550>.
- [29] M. S. Rasheed and S. Shihab, "Analysis of Mathematical Modeling of PV Cell with Numerical Algorithm". *Advanced Energy Conversion Materials*, vol. 1 (2) (2020), pp. 70-79. Available from: <http://ojs.wiserpub.com/index.php/AECM/article/view/328>.
- [30] M. A. Sarhan, "Effect of Silicon Solar Cell Physical Factors on Maximum Conversion Efficiency Theoretically and Experimentally", *Insight-Electronic*, vol. 1 (1) (2019), pp. 24-30.
- [31] Muna Muzahim Abbas, Mohammed Rasheed, "Solid State Reaction Synthesis and Characterization of Aluminum Doped Titanium Dioxide Nanomaterials", *Journal of Southwest Jiaotong University*, vol. 55 (2), pp. 1-10.
- [32] M. M. Abbas and M. Rasheed, "Solid State Reaction Synthesis and Characterization of Cu doped TiO₂ Nanomaterials", *Journal of Physics: Conference Series*, IOP Publishing, vol. 1795 (2021) 012059. doi:10.1088/1742-6596/1795/1/012059

- [33] M. RASHEED, S. SHIHAB and O. W. Sabah, "An investigation of the Structural, Electrical and Optical Properties of Graphene-Oxide Thin Films Using Different Solvents", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012052. doi:10.1088/1742-6596/1795/1/012052
- [34] M. Enneffatia, M. Rasheed, B. Louatia, K. Guidaraa, S. Shihab and R. Barillé, "Investigation of structural, morphology, optical properties and electrical transport conduction of $\text{Li}_0.25\text{Na}_0.75\text{CdVO}_4$ compound", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012050. doi:10.1088/1742-6596/1795/1/012050.
- [35] M. Rasheed, O. Y. Mohammed, S. Shihab and Aqeel Al-Adili, "A comparative Analysis of PV Cell Mathematical Model", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012042. doi:10.1088/1742-6596/1795/1/012042
- [36] M. Rasheed, O. Y. Mohammed, S. Shihab and Aqeel Al-Adili, "Parameters Estimation of Photovoltaic Model Using Nonlinear Algorithms", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012058. doi: 10.1088/1742-6596/1795/1/012058
- [37] M. Rasheed, O. Y. Mohammed, S. Shihab and Aqeel Al-Adili, "Explicit Numerical Model of Solar Cells to Determine Current and Voltage", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012043. doi: 10.1088/1742-6596/1795/1/012043
- [38] A. A. Abdulrahman, M. RASHEED, S. SHIHAB, "The Analytic of image processing smoothing spaces using wavelet", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [39] S. Shihab, M. RASHEED, O. Alabdali and A. A. Abdulrahman, "A Novel Predictor-Corrector Hally Technique for Determining The Parameters for Nonlinear Solar Cell Equation ", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [40] S. Shihab, Bushra E. Kashem, M. A. Sarhan and M. Rasheed, "New Exact Operational Shifted Pell Matrices and Their Application in Astrophysics", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [41] M. RASHEED, S. Shihab, O. Alabdali and H. H. Hussein, "Parameters Extraction of a Single-Diode Model of Photovoltaic Cell Using False Position Iterative Method", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [42] M. RASHEED, O. Alabdali and S. Shihab, "A New Technique for Solar Cell Parameters Estimation of The Single-Diode Model", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [43] M. Rasheed and R. Barillé, "Room temperature deposition of ZnO and Al: ZnO ultrathin films on glass and PET substrates by DC sputtering technique", *Optical and Quantum Electronics*, vol. 49 (5) (2017), pp. 1-14.
- [44] M. Rasheed and Régis Barillé, Optical constants of DC sputtering derived ITO, TiO_2 and TiO_2 : Nb thin films characterized by spectrophotometry and spectroscopic ellipsometry for optoelectronic devices, *Journal of Non-Crystalline Solids*, vol. 476 (2017), pp. 1-14.
- [45] M. Rasheed and R. Barillé, Comparison the optical properties for Bi_2O_3 and NiO ultrathin films deposited on different substrates by DC sputtering technique for transparent electronics, *Journal of Alloys and Compounds*, vol. 728 (2017), pp. 1186-1198.
- [46] M. M. Abbas and M. RASHEED, "Investigation of structural, Mechanical, Thermal and Optical Properties of Cu Doped TiO_2 ", *Iraqi Journal of Physics (IJP)*, (2020), in press.
- [47] M. S. Rasheed, "Approximate Solutions of Barker Equation in Parabolic Orbits", *Engineering & Technology Journal*, vol. 28 (3) (2010), pp. 492-499.
- [48] M. S. Rasheed, "An Improved Algorithm For The Solution of Kepler's Equation For An Elliptical Orbit", *Engineering & Technology Journal*, vol. 28 (7) (2010), pp. 1316-1320.
- [49] M. S. Rasheed, "Acceleration of Predictor Corrector Halley Method in Astrophysics Application", *International Journal of Emerging Technologies in Computational and Applied Sciences*, vol. 1 (2) (2012), pp. 91-94.
- [50] M. S. Rasheed, "Fast Procedure for Solving Two-Body Problem in Celestial Mechanics", *International Journal of Engineering, Business and Enterprise Applications*, vol. 1 (2) (2012), pp. 60-63.
- [51] M. S. Rasheed, "Solve the Position to Time Equation for an Object Travelling on a Parabolic Orbit in Celestial Mechanics", *DIYALA JOURNAL FOR PURE SCIENCES*, vol. 9 (4) (2013), pp. 31-38.
- [52] M. S. Rasheed, "Comparison of Starting Values for Implicit Iterative Solutions to Hyperbolic Orbits Equation", *International Journal of Software and Web Sciences (IJSWS)*, vol. 1 (2) (2013), pp. 65-71.
- [53] M. S. Rasheed, "On Solving Hyperbolic Trajectory Using New Predictor-Corrector Quadrature Algorithms", *Baghdad Science Journal*, vol. 11 (1) (2014), pp. 186-192.
- [54] M. S. Rasheed, "Modification of Three Order Methods for Solving Satellite Orbital Equation in Elliptical Motion", *Journal of university of Anbar for Pure science*, vol. 14 (1) (2020), pp. 33-37.
- [55] Mohammed RASHEED, Suha SHIHAB, Taha RASHEED and Tarek Diab Ounis, "Parameters Determination of PV Cell Using Computation Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 1-9.
- [56] Rasha Jalal Mitlif, Mohammed RASHEED, Suha SHIHAB, Taha RASHEED and Saad Hussein Abed Hamed, "Linear Programming Method Application in a Solar Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 10-21.
- [57] Maiada Nazar Mohammedali, Mohammed RASHEED, Suha SHIHAB, Taha RASHEED and Saad Hussein Abed Hamed, "Optimal Parameters Estimation of Silicon Solar Cell Using Fuzzy Logic: Analytical Method", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 22-33.
- [58] Mohammed RASHEED, Osama Alabdali, Suha SHIHAB and Taha RASHID, "Evaluation and Determination of the Parameters of a Photovoltaic Cell by an Iterative Method", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 34-42.
- [59] M. RASHEED, S. SHIHAB, T. RASHID and T. D. Ounis, "Determination of PV Model Parameters Using Bisection and Secant Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13, (1), (2021), 43-54.
- [60] Raghad I Sabri, Mohammed RASHEED, Osama Alabdali, Suha SHIHAB and Taha RASHID, "On Some Properties in Fuzzy Metric Space", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 55-61.
- [61] Maiada Nazar Mohammedali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Hussein Abed Hamed, "Fuzzy Set Technique Application: The Solar Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 62-69.
- [62] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Olfa Maalej, "Determining the Voltage and Power of a Single Diode PV Cell in Matlab by Iteration", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 70-78.
- [63] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Olfa Maalej, "Numerical Simulation of Photovoltaic Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 79-86.
- [64] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Marwa Enneffati, "Two Numerical Algorithms for Solving Nonlinear Equation of Solar Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 87-94.
- [65] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Marwa Enneffati, "Some Step Iterative Method for Finding Roots of a Nonlinear Equation", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 95-102.
- [66] M. A. Sarhan, S. SHIHAB and M. RASHEED, "Some Results on a Two Variables Pell Polynomials", *Al-Qadisiyah Journal of Pure Science*, vol. 26, (1), (2020), pp. 55-70.

- [67] M. RASHEED, S. SHIHAB and T. RASHID, "Two Step and Newton- Raphson Algorithms in the Extraction for the Parameters of Solar Cell", *Al-Qadisiyah Journal of Pure Science*, vol. 26 (1), (2021), pp.143-154.
- [68] M. A. Sarhan, S. SHIHAB and M. RASHEED, "A novel Spectral Modified Pell Algorithm for Solving Singular Differential Equations", *Al-Mustansiriyah Journal of Science*, vol. 32, (1), (2021), pp. 18-24.
- [69] M. RASHEED, S. SHIHAB and T. RASHID, "Extraction of a Photovoltaic Cell's Single-Diode Model Parameters from Equivalent Circuit", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 147-154.
- [70] M. RASHEED, S. SHIHAB and T. RASHID, "Estimation of Single-Diode Model Parameters of PV Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 139-146.
- [71] M. RASHEED, S. SHIHAB and T. RASHID, "The Single Diode Model for PV Characteristics Using Electrical Circuit", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 131-138.
- [72] R. J. Mitlif, M. Rasheed and S. Shihab, "An Optimal Algorithm for a Fuzzy Transportation Problem", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [73] R. I. Sabri, M. N. Mohammedali, M. Rasheed and S. Shihab, "Compactness of Soft Fuzzy Metric Space", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [74] B. E. Kashem, E. H. Ouda, S. H. Aziz, M. Rasheed and S. Shihab, "Some Results for Orthonormal Boubaker Polynomials with Application", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [75] M. N. Mohammedali, R. I. Sabri, M. Rasheed and S. Shihab, "Some Results on G-Normed Linear Spaces", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [76] T. Saidani, M. Zaabat, M. S. Aida, R. Barille, M. Rasheed, Y. Almohamed, Influence of precursor source on sol-gel deposited ZnO thin films properties, *Journal of Materials Science: Materials in Electronics*, vol. 28 (13) (2017), pp. 9252-9257.
- [77] K. Guergouria A. Boumezoued, R. Barille, D. Rechem, M. Rasheed M. Zaabata, ZnO nanopowders doped with bismuth oxide, from synthesis to electrical application, *Journal of Alloys and Compounds*, vol. 791 (2019), pp. 550-558.
- [78] D. Bouras, A. Mecif, R. Barillé, A. Harabi, M. Rasheed, A. Mahdjoub, M. Zaabat, Cu: ZnO deposited on porous ceramic substrates by a simple thermal method for photocatalytic application, *Ceramics International*, vol. 44 (17) (2018), pp. 21546-21555.
- [79] W. Saidi, N. Hfaïdh, M. Rasheed, M. Girtan, A. Megriche, M. EL Maaoui, Effect of B2O3 addition on optical and structural properties of TiO2 as a new blocking layer for multiple dye sensitive solar cell application (DSSC), *RSC Advances*, vol. 6 (73) (2016), pp. 68819-68826.
- [80] A. AUKSTUOLIS, M. Girtan, G. A. Mousdis, R. Mallet, M. Socol, M. Rasheed, A. Stanculescu, Measurement of charge carrier mobility in perovskite nanowire films by photo-CELIV method, *Proceedings of the Romanian Academy Series a-Mathematics Physics Technical Sciences Information Science*, vol. 18 (1) (2017), pp. 34-41.
- [81] F. Dkhalalli, S. Megdiche, K. Guidara, M. Rasheed, R. Barillé, M. Megdiche, AC conductivity evolution in bulk and grain boundary response of sodium tungstate Na₂WO₄, *Ionics*, vol. 24 (1) (2018), pp. 169-180.
- [82] F. Dkhalalli, S. M. Borchani, M. Rasheed, R. Barille, K. Guidara, M. Megdiche, Structural, dielectric, and optical properties of the zinc tungstate ZnWO₄ compound, *Journal of Materials Science: Materials in Electronics*, vol. 29 (8) (2018), pp. 6297-6307.
- [83] F. Dkhalalli, S. M. Borchani, M. Rasheed, R. Barille, S. Shihab, K. Guidara, M. Megdiche, Characterizations and morphology of sodium tungstate particles, *Royal Society open science*, vol. 5 (8) (2018), pp. 1-12.
- [84] M. Enneffati, B. Louati, K. Guidara, M. Rasheed, R. Barillé, Crystal structure characterization and AC electrical conduction behavior of sodium cadmium orthophosphate, *Journal of Materials Science: Materials in Electronics*, vol. 29 (1) (2018), pp. 171-179.
- [85] E. Kadri, M. Krichen, R. Mohammed, A. Zouari, K. Khirouni, Electrical transport mechanisms in amorphous silicon/crystalline silicon germanium heterojunction solar cell: impact of passivation layer in conversion efficiency, *Optical and Quantum Electronics*, vol. 48 (12) (2016), pp. 1-15.
- [86] E. Kadri, O. Messaoudi, M. Krichen, K. Dhahri, M. Rasheed, E. Dhahri, A. Zouari, K. Khirouni, R. Barillé, Optical and electrical properties of SiGe/Si solar cell heterostructures: Ellipsometric study, *Journal of Alloys and Compounds*, vol. 721 (2017), pp. 779-783.
- [87] E. Kadri, K. Dhahri, A. Zaafouri, M. Krichen, M. Rasheed, K. Khirouni, R. Barillé, Ac conductivity and dielectric behavior of a-Si:H/c-Si_{1-y}Gey/p-Si thin films synthesized by molecular beam epitaxial method, *Journal of Alloys and Compounds*, vol. 705 (2017), pp. 708-713.
- [88] N. B. Azaza, S. Elleuch, M. Rasheed, D. Gindre, S. Abid, R. Barille, Y. Abid, H. Ammar, 3-(p-nitrophenyl) Coumarin derivatives: Synthesis, linear and nonlinear optical properties, *Optical Materials*, vol. 96, (2019), pp. 109328.
- [89] M. Enneffati, M. Rasheed, B. Louati, K. Guidara, R. Barillé, Morphology, UV-visible and ellipsometric studies of sodium lithium orthovanadate, *Optical and Quantum Electronics*, vol. 51 (9) (2019), vol. 299.
- [90] Ali Hasan Ali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Abed Hamad, "A Novel Blurring and Sharpening Techniques Using Different Images Based on Heat Equations", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 45-57.
- [91] Ali Hasan Ali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Abed Hamad, "A Modified Heat Diffusion Based Method for Enhancing Physical Images", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 77-87.
- [92] Ali Hasan Ali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Abed Hamad, "An Effective Color Image Detecting Method for Colorful and Physical Images", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 88-98.
- [93] M. RASHEED, S. SHIHAB and T. RASHID, "Numerical Solving for Nonlinear Problems Using Iterative Techniques", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 201-209.
- [94] M. RASHEED, S. SHIHAB and T. RASHID, "An Accurate and Fast Computational Algorithm Based on Hybrid Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 173-183.
- [95] M. RASHEED, S. SHIHAB and T. RASHID, "Predictor-Corrector Solutions for Nonlinear Equations", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 210-218.
- [96] M. RASHEED, S. SHIHAB and T. RASHID, "Comparison Study Between Classic Chord and Inverse Quadratic Interpolation Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 184-192.