

Numerical Solving for Nonlinear Problems Using Iterative Techniques

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ABSTRACT

Three numerically algorithms are described and compared; newton's; Predictor-Corrector Hally and Accelerated Predictor-Corrector Hally methods have been applied in the present work. Algorithm development for solving the voltage of a solar cell based on it's a single diode equation; programmed using Matlab language. This example is given for induced the idea of this algorithm with the various values of load resistance. The results indicated the suggested algorithm is more efficient with the comparison with other two algorithms.

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1. Introduction

Numerical analysis occupies a prominent position in engineering and physical sciences, because of the relationships and laws governing the variables of a matter of physical or geometry appear in the form of a cocktail non-linear equations or differential equations or partial equations, etc. To understand this issue must be solved. Methods for the solutions of numerical nonlinear equations of the single diode equation of a PV cell depend on the equivalent circuit of a solar cells have been proposed by many applications. The researchers were able to solve many physical, engineering, or even medical problems using many different methods of numerical analysis [1-96].

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In this paper, describes a new algorithm Accelerated Predictor-Corrector Hally method (AHM); so that the nonlinear equation of a solar cell can be solved. It is systematic points: section two characterizing a design of a PV cell (single diode). Section three foundations the zeros finding of Newton Raphson technique. In section four Predictor-Corrector Hally methods has been described. Thus, in section 5 Accelerated Predictor-Corrector Hally method has been demonstrated here; in section six results and discussion are reported while in section seven the conclusions is presented.

2. Design of a Non-Linear Equation

Figure 1 presents PV cell an equivalent circuit (single diode model)

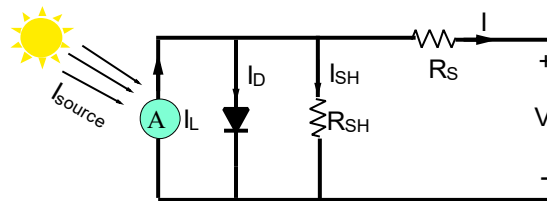


Fig. 1 – PV cell electrical equivalent circuit.

By applying KCL-Kirchhoff's current law on Figure 1; a final equation of the PV cell current is extracted according to this equivalent as follows

$$I = I_{ph} - I_D \tag{1}$$

$$I_D = I_0(e^{-V_{pv}/nV_T} - 1) \tag{2}$$

$$I = I_{ph} - I_0 \times (e^{-V_{pv}/nV_T} - 1) \tag{3}$$

where:

I_{ph} , k , $V_T = kT/q = 26 \text{ mV}$, q , T , I_0 and $1 < m < 2$: the photocurrent (A), Boltzmann constant= $1.38 \times 10^{-23} \text{ J/K}$, thermic voltage, the electron charge= $1.6 \times 10^{-19} \text{ C}$, temperature (K), reverse saturation current and the recombination factor, respectively.

$$I_{ph} = I_{source} \tag{4}$$

$$I_D = I_s * \left(e^{\frac{V_D}{nV_T}} - 1 \right) \tag{5}$$

Subs. Eq. 4 in Eq. 5 yield

$$(I_{source}) - 10^{-12}(\exp(-V/1.2 * 0.026) - 1) = V/R \tag{6}$$

where I_s reverse saturation current= 10^{-12} A . In parallel, $V_D = V = V_{pv}$

Based on the first derivative of Eq. 6; V can be determined numerically.

3. Newton's Method

The following algorithm suggestion for solving Eq. 6 by using NRM

INPUT initial approximate solution $x_0 = 1$,

OUTPUT x_{n+1}

Step 1- Set $x = 0$

Step 2- while $i \leq x_0$

Step 3- Calculate

$$x_{n+1} = x_n - \frac{f(x_n)}{\hat{f}(x_n)} \text{ for } n = 0, 1, 2, \dots \quad (7)$$

Step 4- $|x_i - x_{i-1}| < \varepsilon$; then x_{n+1} and stop.

Step 5- $i = i + 1$, $n = n + 1$, and return to step 2.

Step 6- OUTPUT

4. Predictor – Corrector Halley's Method (HM)

Method 2: Predictor- Corrector Halley's Method (HM)

$$y_n = x_n - (f(x_n)/\hat{f}(x_n)) \quad (8)$$

$$x_{n+1} = y_n - \left(2 \times f(y_n)\hat{f}(y_n)/2 \times \hat{f}(y_n)^2 - f(y_n) \times \hat{f}(y_n) \right) \quad (9)$$

5. Accelerated Predictor-Corrector Halley's Method (AHM)

To compare the different numerical methods of iterations, algorithm 1 and algorithm 2 has been used against the proposed algorithm 3. In addition; Eq. 6. has been solved to demonstrate the performance of the new proposed algorithm and determine the consistency and stability of results. The results are examined using three iterative algorithms

Algorithm 1: Newton Raphson Method (NRM)

$$x_{n+1} = x_n - \frac{f(x_n)}{\hat{f}(x_n)}, n = 0, 1, 2, 3, \dots \quad (10)$$

Algorithm 2: Predictor- Corrector Hally Method (HM)

$$y_n = x_n - \frac{f(x_n)}{\hat{f}(x_n)} \quad (11)$$

$$x_{n+1} = y_n - \frac{2 \times f(y_n)\hat{f}(y_n)}{2 \times \hat{f}(y_n)^2 - f(y_n) \times \hat{f}(y_n)} \quad (12)$$

Algorithm 3: Accelerated Predictor- Corrector Hally Method (AHM)

$$y_n = x_n - \frac{f(x_n)}{\hat{f}(x_n)} \quad (13)$$

$$x_{n+1} = y_n - \frac{2 \times f(y_n)\hat{f}(y_n)}{2 \times \hat{f}(y_n)^2 - f(y_n) \times \hat{f}(y_n)}, n = 0, 1, 2, 3, \dots \quad (14)$$

$$z_n = x_n - \frac{(x_{n+1} - x_n)^2}{x_{n+2} - 2 \times x_{n+1} + x_n}, n = 0, 1, 2, 3, \dots \quad (15)$$

$$\text{Tolerance } \varepsilon = 10^{-9} \text{ and } \sigma = |z_{n+1} - z_n| < \varepsilon, |f(z_n)| < \varepsilon \quad (16)$$

6. Results and Discussion

Three techniques are given by Eqns. 10, 12 and 15 is implemented in order to solve the roots of Eq. 6 which is a non-linear equation with predict guess x_0 . To demonstrate the performance of the three algorithms is used. The approximate solutions produced by the techniques regarded and list the errors acquired by the three techniques. Five different cases are used with the use of Eq. 6 which are based on the R_L values from (1-5) ohm (load resistance)

Tables 1-5 and Figures 2-6. The results indicate AHM need 6 iterations whereas NRM and HM need 9 and 8 iterations respectively for reaching the convergence, this prove that AHM is better than NRM and HM.

Table 1 - Performance indicators for the three different methods (NRM, HM and AHM) identified Eq. 6.

Iterations	V_{pv} -NRM	I_{pv} - NRM	P_{pv} -NRM	V_{pv} -HM	I_{pv} -HM	P_{pv} - HM	V_{pv} -AHM	I_{pv} -AHM	P_{pv} - AHM
1	1	1	1	0.97141684	0.97141684	0.943650676	0.893473351	0.893473351	0.79829463
2	0.971416861	0.971416861	0.943650719	0.946732533	0.946732533	0.89630249	0.918974893	0.918974893	0.844514854
3	0.946732606	0.946732606	0.896302627	0.929865621	0.929865621	0.864650074	0.922319869	0.922319869	0.850673942
4	0.929865706	0.929865706	0.864650231	0.923247877	0.923247877	0.852386643	0.922422989	0.922422989	0.850864171
5	0.923247893	0.923247893	0.852386673	0.922434	0.922434	0.850884484	0.922423135	0.922423135	0.850864439
6	0.922434	0.922434	0.850884484	0.922423136	0.922423136	0.850864443	0.922423135	0.922423135	0.850864439
7	0.922423136	0.922423136	0.850864443	0.922423135	0.922423135	0.850864439			
8	0.922423135	0.922423135	0.850864439	0.922423135	0.922423135	0.850864439			
9	0.922423135	0.922423135	0.850864439						

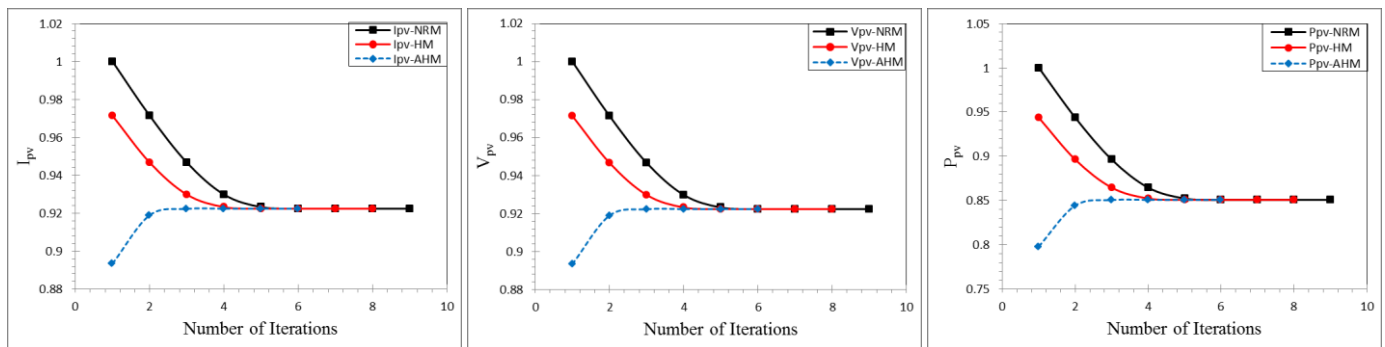


Fig. 2 - Predicted PV parameters from experimental data.

Table 2 - Performance indicators for the three different methods (NRM, HM and AHM) identified Eq. 6.

Iterations	V_{pv} -NRM	I_{pv} - NRM	P_{pv} -NRM	V_{pv} -HM	I_{pv} -HM	P_{pv} - HM	V_{pv} -AHM	I_{pv} -AHM	P_{pv} - AHM
1	1	0.5	0.5	0.971030449	0.485515224	0.471450066	0.877625589	0.438812794	0.385113337
2	0.97103047	0.48551524	0.47145009	0.945421879	0.47271094	0.446911265	0.911522753	0.455761377	0.415436865
3	0.94542197	0.47271098	0.44691135	0.926834345	0.463417173	0.429510952	0.916798952	0.458399476	0.420260159
4	0.92683448	0.46341724	0.42951107	0.918438709	0.459219354	0.421764831	0.917034659	0.458517329	0.420476283
5	0.91843875	0.45921937	0.42176486	0.917066884	0.458533442	0.420505835	0.917035382	0.458517691	0.420476946
6	0.91706688	0.45853344	0.42050584	0.917035399	0.458517699	0.420476961	0.917035382	0.458517691	0.420476946
7	0.9170354	0.4585177	0.42047696	0.917035382	0.458517691	0.420476946			
8	0.91703538	0.45851769	0.42047695	0.917035382	0.458517691	0.420476946			
9	0.91703538	0.45851769	0.42047695						

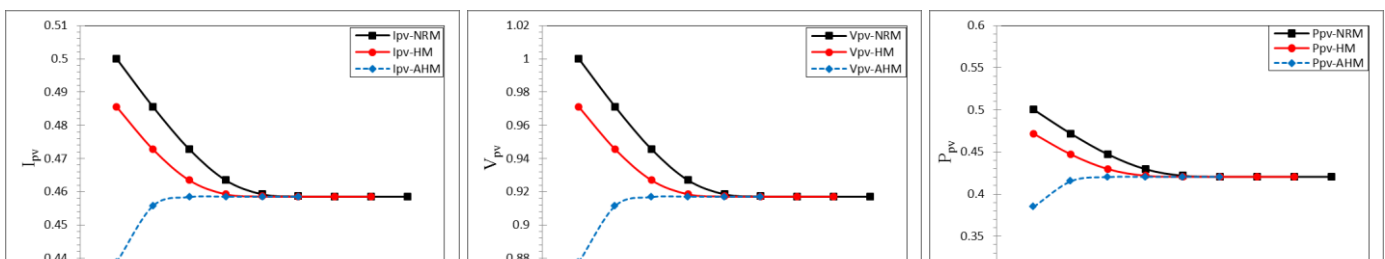


Fig. 3 - Predicted PV parameters from experimental data.

Table 3 - Performance indicators for the three different methods (NRM, HM and AHM) identified Eq. 6.

Iterations	V_{pv} -NRM	I_{pv} -NRM	P_{pv} -NRM	V_{pv} -HM	I_{pv} -HM	P_{pv} -HM	V_{pv} -AHM	I_{pv} -AHM	P_{pv} -AHM
1	1	0.333333333	0.333333333	0.970643767	0.323547922	0.314049774	0.854421872	0.284807291	0.243345578
2	0.970643792	0.323547931	0.31404979	0.944084126	0.314694709	0.297098279	0.901128093	0.300376031	0.27067728
3	0.944084232	0.314694744	0.297098346	0.923594034	0.307864678	0.28434198	0.909824059	0.303274686	0.275926606
4	0.923594243	0.307864748	0.284342109	0.912877747	0.304292582	0.277781927	0.91039934	0.303466447	0.276275653
5	0.91287784	0.304292613	0.277781984	0.910501258	0.303500419	0.276337514	0.910403374	0.303467791	0.276278101
6	0.910501262	0.303500421	0.276337516	0.910403531	0.303467844	0.276278197	0.910403374	0.303467791	0.276278101
7	0.910403531	0.303467844	0.276278197	0.910403374	0.303467791	0.276278101			
8	0.910403374	0.303467791	0.276278101	0.910403374	0.303467791	0.276278101			
9	0.910403374	0.303467791	0.276278101						

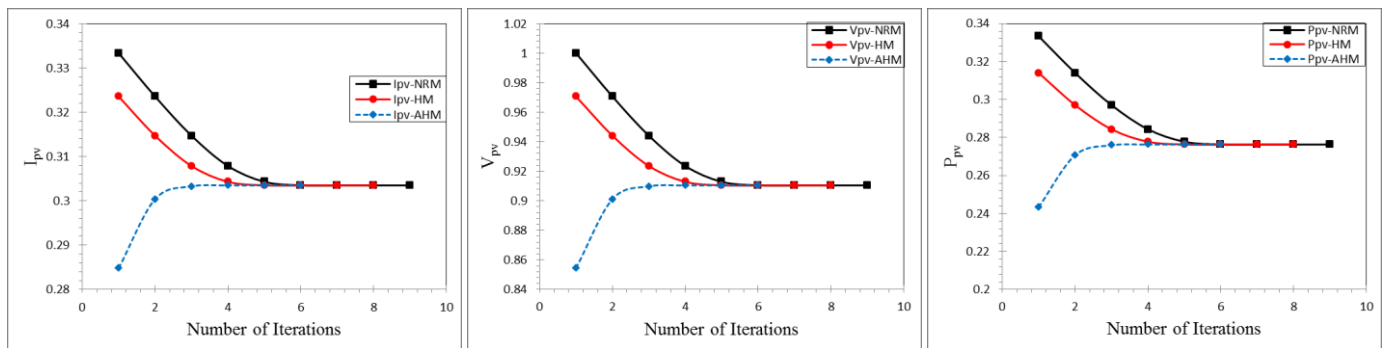


Fig. 4 - Predicted PV parameters from experimental data.

Table 4 - Performance indicators for the three different methods (NRM, HM and AHM) identified Eq. 6.

Iterations	V_{pv} -NRM	I_{pv} -NRM	P_{pv} -NRM	V_{pv} -HM	I_{pv} -HM	P_{pv} -HM	V_{pv} -AHM	I_{pv} -AHM	P_{pv} -AHM
1	1	0.25	0.25	0.970256795	0.242564199	0.235349562	0.816814932	0.204203733	0.166796658
2	0.970256822	0.242564205	0.235349575	0.942718592	0.235679648	0.222179586	0.884826813	0.221206703	0.195729622
3	0.94271872	0.23567968	0.222179646	0.920122669	0.230030667	0.211656431	0.900161317	0.225040329	0.202572599
4	0.920123009	0.230030752	0.211656588	0.906346232	0.226586558	0.205365873	0.901713941	0.225428485	0.203272008
5	0.906346494	0.226586624	0.205365992	0.902077679	0.22551942	0.203436035	0.901740591	0.225435148	0.203284023
6	0.902077706	0.225519427	0.203436047	0.901742503	0.225435626	0.203284885	0.901740602	0.22543515	0.203284028

7	0.901742503	0.225435626	0.203284885	0.901740602	0.225435151	0.203284028			
8	0.901740602	0.225435151	0.203284028	0.901740602	0.22543515	0.203284028			
9	0.901740602	0.22543515	0.203284028						

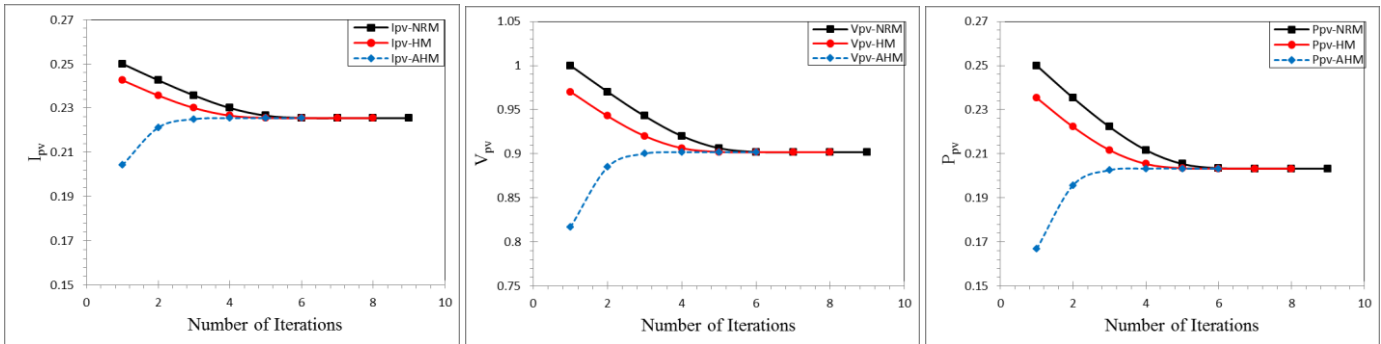


Fig. 5 - Predicted PV parameters from experimental data.

Table 5 - Performance indicators for the three different methods (NRM, HM and AHM) identified Eq. 6.

Iterations	V_{pv} -NRM	I_{pv} -NRM	P_{pv} -NRM	V_{pv} -HM	I_{pv} -HM	P_{pv} -HM	V_{pv} -AHM	I_{pv} -AHM	P_{pv} -AHM
1	1	0.2	0.2	0.969869532	0.193973906	0.188129382	0.744511944	0.148902389	0.110859607
2	0.96986956	0.193973912	0.188129393	0.941324576	0.188264915	0.177218391	0.853407466	0.170681493	0.145660861
3	0.941324731	0.188264946	0.17721845	0.916395271	0.183279054	0.167956059	0.883852721	0.176770544	0.156239126
4	0.916395843	0.183279169	0.167956268	0.898534787	0.179706957	0.161472953	0.888853623	0.177770725	0.158012153
5	0.898535645	0.179707129	0.161473261	0.890476758	0.178095352	0.158589771	0.889091907	0.177818381	0.158096884
6	0.890477009	0.178095402	0.158589861	0.889125756	0.177825151	0.158108922	0.889092715	0.177818543	0.158097171
7	0.889125763	0.177825153	0.158108925	0.889092734	0.177818547	0.158097178	0.889092715	0.177818543	0.158097171
8	0.889092734	0.177818547	0.158097178	0.889092715	0.177818543	0.158097171			
9	0.889092715	0.177818543	0.158097171	0.889092715	0.177818543	0.158097171			
10	0.889092715	0.177818543	0.158097171						

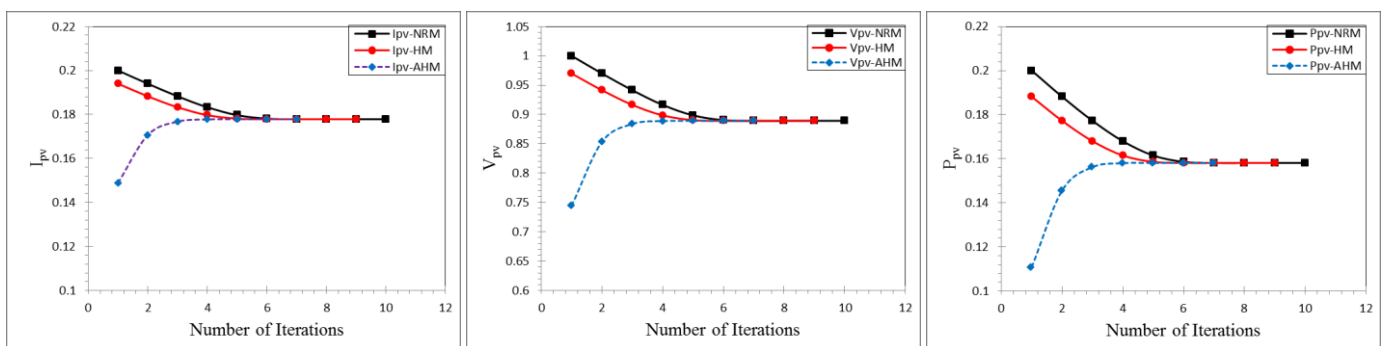


Fig. 6 - Predicted PV parameters from experimental data.

7. Conclusion

A new Accelerated Predictor- Corrector Hally method is introduced in order to obtain the numerical solutions of a single diode equivalent circuit design with a different values of load resistance R. Several algorithms (NRM, HM and AHM) were applied for illustration and good results were achieved for the calculations of the voltage of a solar cell. The following steps have been identified: First, the process of computation presented of a new proposed

algorithm in the equation of a solar cell approach is simple; the approximate results are easy to obtain by a few computations; so the approach is considerably powerful. Second Good results obtained depend on the selection of the initial value x_0 for the three algorithms. Third Good results based on the algorithms used to find the involved model.

References

- [1] M. M. Delphi and S. N. Shihab, "State Parameterization Basic Spline Functions for Trajectory Optimization", *Journal of Nature, Life and Applied Sciences*, vol. 3 (4) (2019), pp. 110-119.
- [2] S. Shihab and M. Delphi, "Direct Iterative Algorithm for Solving Optimal Control Problems Using B-Spline Polynomials", *Emirates Journal for Engineering Research*, vol. 24 (4) (2019), pp. 1-9.
- [3] M. Delphi and S. Shihab, "Modified Iterative Algorithm for Solving Optimal Control Problems", *Open Science Journal of Statistics and Application*, vol. 6 (2) (2019), pp. 20-27.
- [4] S. N. Shihab, A. A. Abdulrahman and M. N. Mohammed Ali, "Collocation Orthonormal Bernstein Polynomials Method for Solving Integral Equations", *Engineering and Technology Journal*, vol. 33 (8) (2015), pp. 1493-1502.
- [5] S. N. Shihab and T. N. Naif, "On the orthonormal Bernstein polynomial of order eight", *Open Science Journal of Mathematics and Application*, vol. 2 (2) (2014), pp. 15-19.
- [6] S. N. Shihab and A. A. Abdulrahman, "Solving Optimal Control Linear Systems by Using New Third kind Chebyshev Wavelets Operational Matrix of Derivative", *Baghdad Science Journal*, vol. 11 (2) (2014), pp. 229-234.
- [7] S. N. Shihab and A. A. Abdulrahman, "Some New Relationships Between the Derivatives of First and Second Chebyshev Wavelets", *International Journal of Engineering, Business and Enterprise Application*, (2012), pp. 64-68.
- [8] S. N. Shihab and A. A. Abdulrahman, "Numerical solution of calculus of variations by using the second Chebyshev wavelets", *Engineering and Technology Journal*, vol. 30 (18) (2012), pp. 3219-3229.
- [9] S. N. Shehab, H. A. Ali, H. M. Yaseen, "Least squares method for solving integral equations with multiple time lags", *Engineering & Technology Journal*, vol. 28 (10) (2010), pp. 1893-1899.
- [10] S. N. Al-Rawi, "On the Solution of Certain Fractional Integral Equations", *Journal of Kirkuk University–Scientific Studies*, vol. 1 (2) (2006).
- [11] S. N. Al-Rawi, R. K. Salih and A. A. Mohammed, "Numerical Solution of Nth Order Linear Delay Differential Equation Using Runge-Kutta Method", *Um - Salama Science Journal*, vol. 3 (1) (2006), pp. 140-146.
- [12] M. RASHEED, A. A. Abdulrahman, and S. Shihab, "The Effect of Set Partitioning in Hierarchical Trees with Wavelet Decomposition Levels Algorithm for Image Compression", *Electronics Science Technology and Application*, vol. 7 (3) (2020), pp. 40-46.
- [13] A. A. Abdulrahman, M. RASHEED and S. SHIHAB, "Various Techniques for De-noise Image, Electronics Science Technology and Application, vol. 7 (4) (2020), pp. 79-84.
- [14] A. A. Abdulrahman, M. RASHEED and S. SHIHAB, "Discrete Hermite Wavelet Filters with Prove Mathematical Aspects", *Journal of Southwest Jiaotong University*, vol. 55 (2) (2020), pp. 1-12.
- [15] A. A. Abdulrahman, M. RASHEED and S. SHIHAB, "Discrete Chebyshev Wavelet Transformation with Image Processing", *Journal of Southwest Jiaotong University*, vol. 55 (2) (2020), pp. 1-17.
- [16] M. S. Rasheed, H. S. Mahde, "Electronic Combination Lock Design Using Remote Control", *Journal of the College of Basic Education*, vol. 18 (75) (2012), pp. 265-280.
- [17] M. S. Rasheed and Balqis M. Diah, "Study of the effects of acidic solutions on the physical properties of polymeric materials superimposed", *Al-Mustansiriyah Journal of Science*, vol. 13 (49) (2002), pp. 6.
- [18] M. RASHEED and M. A. Sarhan, "Solve and Implement the main Equations of Photovoltaic Cell Parameters Using Visual Studio Program", *Insight-Mathematics*, vol. 1 (1) (2019), pp. 17-25.
- [19] M. Rasheed and M. A. Sarhan, "Characteristics of Solar Cell Outdoor Measurements Using Fuzzy Logic Method", *Insight-Mathematics*, vol. 1 (1) (2019), pp. 1-8.
- [20] M. RASHEED and M. A. Sarhan, "Measuring the Solar Cell Parameters Using Fuzzy Set Technique", *Insight-Electronic*, vol. 1 (1) (2019), pp. 1-9.
- [21] M. RASHEED, "Linear Programming for Solving Solar Cell Parameters", *Insight-Electronic*, vol. 1 (1) (2019), pp. 10-16.
- [22] M. RASHEED, "Investigation of Solar Cell Factors using Fuzzy Set Technique", *Insight-Electronic*, vol. 1 (1) (2019), pp. 17-23.
- [23] M. RASHEED and S. SHIHAB, "Analytical Modeling of Solar Cells", *Insight Electronics*, vol. 1 (2) (2019), pp. 1-9.
- [24] S. SHIHAB and M. RASHEED, "Modeling and Simulation of Solar Cell Mathematical Model Parameters Determination Based on Different Methods", *Insight Mathematics*, vol. 1 (1) (2019), pp. 1-16.
- [25] M. RASHEED and S. SHIHAB, "Parameters Estimation for Mathematical Model of Solar Cell", *Electronics Science Technology and Application*, vol. 6, (1) (2019), pp. 20-28.
- [26] M. Rasheed and S. Shihab, "Numerical Techniques for Solving Parameters of Solar Cell", *Applied Physics*, vol. 3 (1) (2020), pp. 16-27.
- [27] M. RASHEED and S. SHIHAB, "Modifications to Accelerate the Iterative Algorithm for the Single Diode Model of PV Model", *Iraqi Journal of Physics (IJP)*, vol. 18 (47) (2020), pp. 33-43.
- [28] M. S. Rasheed and S. Shihab, "Modelling and Parameter Extraction of PV Cell Using Single-Diode Model". *Advanced Energy Conversion Materials*, 1 (2) (2020), pp. 96-104. Available from: <http://ojs.wiserpub.com/index.php/AECM/article/view/550>.
- [29] M. S. Rasheed and S. Shihab, "Analysis of Mathematical Modeling of PV Cell with Numerical Algorithm". *Advanced Energy Conversion Materials*, vol. 1 (2) (2020), pp. 70-79. Available from: <http://ojs.wiserpub.com/index.php/AECM/article/view/328>.
- [30] M. A. Sarhan, "Effect of Silicon Solar Cell Physical Factors on Maximum Conversion Efficiency Theoretically and Experimentally", *Insight-Electronic*, vol. 1 (1) (2019), pp. 24-30.
- [31] Muna Muzahim Abbas, Mohammed Rasheed, "Solid State Reaction Synthesis and Characterization of Aluminum Doped Titanium Dioxide Nanomaterials", *Journal of Southwest Jiaotong University*, vol. 55 (2), pp. 1-10.
- [32] M. M. Abbas and M. Rasheed, "Solid State Reaction Synthesis and Characterization of Cu doped TiO₂ Nanomaterials", *Journal of Physics: Conference Series*, IOP Publishing, vol. 1795 (2021) 012059. doi:10.1088/1742-6596/1795/1/012059

- [33] M. RASHEED, S. SHIHAB and O. W. Sabah, "An investigation of the Structural, Electrical and Optical Properties of Graphene-Oxide Thin Films Using Different Solvents", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012052. doi:10.1088/1742-6596/1795/1/012052
- [34] M. Enneffatia, M. Rasheed, B. Louatia, K. Guidaraa, S. Shihab and R. Barillé, "Investigation of structural, morphology, optical properties and electrical transport conduction of $\text{Li}_0.25\text{Na}_0.75\text{CdVO}_4$ compound", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012050. doi:10.1088/1742-6596/1795/1/012050.
- [35] M. Rasheed, O. Y. Mohammed, S. Shihab and Aqeel Al-Adili, "A comparative Analysis of PV Cell Mathematical Model", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012042. doi:10.1088/1742-6596/1795/1/012042
- [36] M. Rasheed, O. Y. Mohammed, S. Shihab and Aqeel Al-Adili, "Parameters Estimation of Photovoltaic Model Using Nonlinear Algorithms", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012058. doi: 10.1088/1742-6596/1795/1/012058
- [37] M. Rasheed, O. Y. Mohammed, S. Shihab and Aqeel Al-Adili, "Explicit Numerical Model of Solar Cells to Determine Current and Voltage", *Journal of Physics: Conference Series*. IOP Publishing, 1795 (2021) 012043. doi: 10.1088/1742-6596/1795/1/012043
- [38] A. A. Abdulrahman, M. RASHEED, S. SHIHAB, "The Analytic of image processing smoothing spaces using wavelet", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [39] S. Shihab, M. RASHEED, O. Alabdali and A. A. Abdulrahman, "A Novel Predictor-Corrector Hally Technique for Determining The Parameters for Nonlinear Solar Cell Equation", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [40] S. Shihab, Bushra E. Kashem, M. A. Sarhan and M. Rasheed, "New Exact Operational Shifted Pell Matrices and Their Application in Astrophysics", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [41] M. RASHEED, S. Shihab, O. Alabdali and H. H. Hussein, "Parameters Extraction of a Single-Diode Model of Photovoltaic Cell Using False Position Iterative Method", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [42] M. RASHEED, O. Alabdali and S. Shihab, "A New Technique for Solar Cell Parameters Estimation of The Single-Diode Model", *Journal of Physics: Conference Series*. IOP Publishing, (2021), in press.
- [43] M. Rasheed and R. Barillé, "Room temperature deposition of ZnO and Al: ZnO ultrathin films on glass and PET substrates by DC sputtering technique", *Optical and Quantum Electronics*, vol. 49 (5) (2017), pp. 1-14.
- [44] M. Rasheed and Régis Barillé, Optical constants of DC sputtering derived ITO, TiO_2 and TiO_2 : Nb thin films characterized by spectrophotometry and spectroscopic ellipsometry for optoelectronic devices, *Journal of Non-Crystalline Solids*, vol. 476 (2017), pp. 1-14.
- [45] M. Rasheed and R. Barillé, Comparison the optical properties for Bi_2O_3 and NiO ultrathin films deposited on different substrates by DC sputtering technique for transparent electronics, *Journal of Alloys and Compounds*, vol. 728 (2017), pp. 1186-1198.
- [46] M. M. Abbas and M. RASHEED, "Investigation of structural, Mechanical, Thermal and Optical Properties of Cu Doped TiO_2 ", *Iraqi Journal of Physics (IJP)*, (2020), in press.
- [47] M. S. Rasheed, "Approximate Solutions of Barker Equation in Parabolic Orbits", *Engineering & Technology Journal*, vol. 28 (3) (2010), pp. 492-499.
- [48] M. S. Rasheed, "An Improved Algorithm For The Solution of Kepler's Equation For An Elliptical Orbit", *Engineering & Technology Journal*, vol. 28 (7) (2010), pp. 1316-1320.
- [49] M. S. Rasheed, "Acceleration of Predictor Corrector Halley Method in Astrophysics Application", *International Journal of Emerging Technologies in Computational and Applied Sciences*, vol. 1 (2) (2012), pp. 91-94.
- [50] M. S. Rasheed, "Fast Procedure for Solving Two-Body Problem in Celestial Mechanics", *International Journal of Engineering, Business and Enterprise Applications*, vol. 1 (2) (2012), pp. 60-63.
- [51] M. S. Rasheed, "Solve the Position to Time Equation for an Object Travelling on a Parabolic Orbit in Celestial Mechanics", *DIYALA JOURNAL FOR PURE SCIENCES*, vol. 9 (4) (2013), pp. 31-38.
- [52] M. S. Rasheed, "Comparison of Starting Values for Implicit Iterative Solutions to Hyperbolic Orbits Equation", *International Journal of Software and Web Sciences (IJSWS)*, vol. 1 (2) (2013), pp. 65-71.
- [53] M. S. Rasheed, "On Solving Hyperbolic Trajectory Using New Predictor-Corrector Quadrature Algorithms", *Baghdad Science Journal*, vol. 11 (1) (2014), pp. 186-192.
- [54] M. S. Rasheed, "Modification of Three Order Methods for Solving Satellite Orbital Equation in Elliptical Motion", *Journal of university of Anbar for Pure science*, vol. 14 (1) (2010), pp. 33-37.
- [55] Mohammed RASHEED, Suha SHIHAB, Taha RASHEED and Tarek Diab Ounis, "Parameters Determination of PV Cell Using Computation Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 1-9.
- [56] Rasha Jalal Mitlif, Mohammed RASHEED, Suha SHIHAB, Taha RASHEED and Saad Hussein Abed Hamed, "Linear Programming Method Application in a Solar Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 10-21.
- [57] Maiada Nazar Mohammedali, Mohammed RASHEED, Suha SHIHAB, Taha RASHEED and Saad Hussein Abed Hamed, "Optimal Parameters Estimation of Silicon Solar Cell Using Fuzzy Logic: Analytical Method", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 22-33.
- [58] Mohammed RASHEED, Osama Alabdali, Suha SHIHAB and Taha RASHID, "Evaluation and Determination of the Parameters of a Photovoltaic Cell by an Iterative Method", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 34-42.
- [59] M. RASHEED, S. SHIHAB, T. RASHID and T. D. Ounis, "Determination of PV Model Parameters Using Bisection and Secant Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13, (1), (2021), 43-54.
- [60] Raghad I Sabri, Mohammed RASHEED, Osama Alabdali, Suha SHIHAB and Taha RASHID, "On Some Properties in Fuzzy Metric Space", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 55-61.
- [61] Maiada Nazar Mohammedali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Hussein Abed Hamed, "Fuzzy Set Technique Application: The Solar Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 62-69.
- [62] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Olfa Maalej, "Determining the Voltage and Power of a Single Diode PV Cell in Matlab by Iteration", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 70-78.
- [63] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Olfa Maalej, "Numerical Simulation of Photovoltaic Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 79-86.
- [64] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Marwa Enneffati, "Two Numerical Algorithms for Solving Nonlinear Equation of Solar Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 87-94.
- [65] Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Marwa Enneffati, "Some Step Iterative Method for Finding Roots of a Nonlinear Equation", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 95-102.

- [66] M. A. Sarhan, S. SHIHAB and M. RASHEED, "Some Results on a Two Variables Pell Polynomials", *Al-Qadisiyah Journal of Pure Science*, vol. 26, (1), (2020), pp. 55-70.
- [67] M. RASHEED, S. SHIHAB and T. RASHID, "Two Step and Newton- Raphson Algorithms in the Extraction for the Parameters of Solar Cell", *Al-Qadisiyah Journal of Pure Science*, vol. 26 (1), (2021), pp.143-154.
- [68] M. A. Sarhan, S. SHIHAB and M. RASHEED, "A novel Spectral Modified Pell Algorithm for Solving Singular Differential Equations", *Al-Mustansiriyah Journal of Science*, vol. 32, (1), (2021), pp. 18-24.
- [69] M. RASHEED, S. SHIHAB and T. RASHID, "Extraction of a Photovoltaic Cell's Single-Diode Model Parameters from Equivalent Circuit", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 147-154.
- [70] M. RASHEED, S. SHIHAB and T. RASHID, "Estimation of Single-Diode Model Parameters of PV Cell", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 139-146.
- [71] M. RASHEED, S. SHIHAB and T. RASHID, "The Single Diode Model for PV Characteristics Using Electrical Circuit", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 131-138.
- [72] R. J. Mitlif, M. Rasheed and S. Shihab, "An Optimal Algorithm for a Fuzzy Transportation Problem", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [73] R. I. Sabri, M. N. Mohammedali, M. Rasheed and S. Shihab, "Compactness of Soft Fuzzy Metric Space", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [74] B. E. Kashem, E. H. Ouda, S. H. Aziz, M. Rasheed and S. Shihab, "Some Results for Orthonormal Boubaker Polynomials with Application", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [75] M. N. Mohammedali, R. I. Sabri, M. Rasheed and S. Shihab, "Some Results on G-Normed Linear Spaces", *Journal of Southwest Jiaotong University*, vol. 55 (3), (2020).
- [76] T. Saidani, M. Zaabat, M. S. Aida, R. Barille, M. Rasheed, Y. Almohamed, Influence of precursor source on sol-gel deposited ZnO thin films properties, *Journal of Materials Science: Materials in Electronics*, vol. 28 (13) (2017), pp. 9252-9257.
- [77] K. Guergouria A. Boumezoued, R. Barille, D. Rechenc, M. Rasheed M. Zaabata, ZnO nanopowders doped with bismuth oxide, from synthesis to electrical application, *Journal of Alloys and Compounds*, vol. 791 (2019), pp. 550-558.
- [78] D. Bouras, A. Mecif, R. Barillé, A. Harabi, M. Rasheed, A. Mahdjoub, M. Zaabat, Cu: ZnO deposited on porous ceramic substrates by a simple thermal method for photocatalytic application, *Ceramics International*, vol. 44 (17) (2018), pp. 21546-21555.
- [79] W. Saidi, N. Hfaïdh, M. Rasheed, M. Girtan, A. Megriche, M. EL Maaoui, Effect of B2O3 addition on optical and structural properties of TiO2 as a new blocking layer for multiple dye sensitive solar cell application (DSSC), *RSC Advances*, vol. 6 (73) (2016), pp. 68819-68826.
- [80] A. AUKSTUOLIS, M. Girtan, G. A. Mousdis, R. Mallet, M. Socol, M. Rasheed, A. Stanculescu, Measurement of charge carrier mobility in perovskite nanowire films by photo-CELIV method, *Proceedings of the Romanian Academy Series a-Mathematics Physics Technical Sciences Information Science*, vol. 18 (1) (2017), pp. 34-41.
- [81] F. Dkhalalli, S. Megdiche, K. Guidara, M. Rasheed, R. Barillé, M. Megdiche, AC conductivity evolution in bulk and grain boundary response of sodium tungstate Na₂WO₄, *Ionics*, vol. 24 (1) (2018), pp. 169-180.
- [82] F. Dkhalalli, S. M. Borchani, M. Rasheed, R. Barille, K. Guidara, M. Megdiche, Structural, dielectric, and optical properties of the zinc tungstate ZnWO₄ compound, *Journal of Materials Science: Materials in Electronics*, vol. 29 (8) (2018), pp. 6297-6307.
- [83] F. Dkhalalli, S. M. Borchani, M. Rasheed, R. Barille, S. Shihab, K. Guidara, M. Megdiche, Characterizations and morphology of sodium tungstate particles, *Royal Society open science*, vol. 5 (8) (2018), pp. 1-12.
- [84] M. Enneffati, B. Louati, K. Guidara, M. Rasheed, R. Barillé, Crystal structure characterization and AC electrical conduction behavior of sodium cadmium orthophosphate, *Journal of Materials Science: Materials in Electronics*, vol. 29 (1) (2018), pp. 171-179.
- [85] E. Kadri, M. Krichen, R. Mohammed, A. Zouari, K. Khirouni, Electrical transport mechanisms in amorphous silicon/crystalline silicon germanium heterojunction solar cell: impact of passivation layer in conversion efficiency, *Optical and Quantum Electronics*, vol. 48 (12) (2016), pp. 1-15.
- [86] E. Kadri, O. Messaoudi, M. Krichen, K. Dhahri, M. Rasheed, E. Dhahri, A. Zouari, K. Khirouni, R. Barillé, Optical and electrical properties of SiGe/Si solar cell heterostructures: Ellipsometric study, *Journal of Alloys and Compounds*, vol. 721 (2017), pp. 779-783.
- [87] E. Kadri, K. Dhahri, A. Zaafour, M. Krichen, M. Rasheed, K. Khirouni, R. Barillé, Ac conductivity and dielectric behavior of a-Si:H/c-Si_{1-y}Gey/p-Si thin films synthesized by molecular beam epitaxial method, *Journal of Alloys and Compounds*, vol. 705 (2017), pp. 708-713.
- [88] N. B. Azaza, S. Elleuch, M. Rasheed, D. Gindre, S. Abid, R. Barille, Y. Abid, H. Ammar, 3-(p-nitrophenyl) Coumarin derivatives: Synthesis, linear and nonlinear optical properties, *Optical Materials*, vol. 96, (2019), pp. 109328.
- [89] M. Enneffati, M. Rasheed, B. Louati, K. Guidara, R. Barillé, Morphology, UV-visible and ellipsometric studies of sodium lithium orthovanadate, *Optical and Quantum Electronics*, vol. 51 (9) (2019), vol. 299.
- [90] Ali Hasan Ali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Abed Hamad, "A Novel Blurring and Sharpening Techniques Using Different Images Based on Heat Equations", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 45-57.
- [91] Ali Hasan Ali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Abed Hamad, "A Modified Heat Diffusion Based Method for Enhancing Physical Images", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 77-87.
- [92] Ali Hasan Ali, Mohammed RASHEED, Suha SHIHAB, Taha RASHID and Saad Abed Hamad, "An Effective Color Image Detecting Method for Colorful and Physical Images", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 88-98.
- [93] M. RASHEED, S. SHIHAB and T. RASHID, "An Accurate and Fast Computational Algorithm Based on Hybrid Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 173-183.
- [94] M. RASHEED, S. SHIHAB and T. RASHID, "Experimental Results for a Nonlinear Equation Using Improved Newton-Raphson Estimation Method", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp.193-200.
- [95] M. RASHEED, S. SHIHAB and T. RASHID, "Predictor-Corrector Solutions for Nonlinear Equations", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 210-218.
- [96] M. RASHEED, S. SHIHAB and T. RASHID, "Comparison Study Between Classic Chord and Inverse Quadratic Interpolation Methods", *Journal of Al-Qadisiyah for Computer Science and Mathematics*, vol. 13 (1), (2021), pp. 184-192.