

Further Acceleration of Two-Point Bracketing Method for Determining the Voltages of Nonlinear Equation

Mohammed RASHEED ^{a,*}, SUHA SHIHAB^b, Ahmed Rashid ^c, Taha Rashid ^d, Saad Hussein Abed Hamad^e, Yasir Ahmed Mohammed Ridha AL-Sabbagh^f

^a Applied Science Department, University of Technology, Baghdad, Iraq, email: rasheed.mohammed40@yahoo.com, mohammed.s.rasheed@uotechnology.edu.iq.

^b Applied Science Department, University of Technology, Baghdad, Iraq, e-mail: alrawy1978@yahoo.com, suha.n.shihab@uotechnology.edu.iq.

^c Al Iraqia University, College of Arts, Baghdad, Iraq, e-mail: dr.ahm.8215@gmail.com, ahmed_rashed@aliraqia.edu.iq.

^d Computer and Microelectronics System, Faculty of Engineering, University of Malaysia, Skudai 81310, Johor Bahru, Malaysia, and Al Iraqia University, College of Arts, Baghdad, Iraq, e-mail: tsiham95@gmail.com, taha1988@graduate.utm.my.

^e College of Computer Science & Information Technology, Al Qadisyah University, Al-Diwaniyah, Iraq, e-mail: shsaadsh2014@gmail.com, saad.hussain@qu.edu.iq.

^f Mechanical Engineering, Faculty of Engineering, University of Malaysia, Skudai 81310, Johor Bahru, Malaysia, e-mail: abed.ola@graduate.utm.my.

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ABSTRACT

A general class of three point iterative algorithms for solving nonlinear equations based on single diode model of a PV cell is constructed in the present work. Three steps iterative methods for solving nonlinear equation of solar cell, Illinois Algorithm and Two-Point Bracketing algorithm are presented and analyzed. In addition; the absolute error values for all the algorithms have been discussed and compared. The new proposed method has the lesser number of iterations than the other ones has been founded. Numerical examples are contained to test and investigate the performance, accuracy and efficiency of these methods.

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*Corresponding author: Mohammed RASHEED

Email addresses: rasheed.mohammed40@yahoo.com , 10606@uotechnology.edu.iq

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1. Introduction

During the last decade, iterative methods for solving nonlinear equations of engineering and science fields have been introduced in many articles. The main aim of these articles were the construction of the iterative methods based on computational efficiency as high as possible, which supposes the structure or style of iterative algorithms having the faster convergence based on the number of evaluations of the functions per iteration. Some iterative algorithms of nonlinear equations using free of second derivatives have been presented and analyzed, and there are many methods improved on the advancement the convergence of the standard iterative method, in order to attain lesser iterations than it [1-115].

The suggested algorithm TPBM requires 6 evaluations of the function while the other technique (IRFM) needs 7 evaluation of the function. The following steps are investigate the procedure of this work: section two, three and four investigating the modeling and the root finding of IRFM and TPBM algorithms respectively while; section five and six indicate the numerical problems, discussion and conclusion results respectively.

2. - Equation : Non-Linear Formula

KCL Kirchhoff's law is employed in order to depict the electrical parameters of PV cell scheme [30-50]

$$I = I_{ph} - I_{Diode}, I_{Diode} = I_0 \left[\exp\left(\frac{-V_{pv}}{nV_T}\right) - 1 \right] \quad (1)$$

where:

I_0 is diode reverse saturation current measured in (A), I_{ph} is light current, n is diode ideality factor (unitless), $k = (1.38 \times 10^{-23} \text{ J/K})$ is Boltzmann constant, $q = (1.602 \times 10^{-19} \text{ C})$ is elementary charge, V_T is thermal voltage given by $V_T = \frac{kT}{q}$, I_{ph} is the light generated current in the cell, T is temperature (p-n junction), I_D is the voltage dependent current lost to recombination.

The current I_{pv} and power P_{pv} of the cell is given by $I_{pv} = \frac{V_{pv}}{R}$; $P_{pv} = I_{pv} \times V_{pv}$

The final equation from the circuit is given by

$$(I_{source}) - 10^{-12} \left(e^{\frac{-V}{1.2 \times 0.026}} - 1 \right) = V / R \quad (2)$$

3. Illinois Algorithm (IRFM)

x_0 is the Initial value, x_{n+1} is the approximation value

Step 1: Suppose $f(x_1) = b_1, f(x_2) = b_2$

Step 2: $f(x) = ax + b$;

$$\text{Step 3: } x = \frac{b_1 x_2 - b_2 x_1}{(b_1 - b_2)} \quad (3)$$

4. Two Point Bracketing Method (TPBM)

Step 1: for a given $[a_k, b_k]$

$$\text{Step 2: compute } c_k \text{ as follows } c_k = \frac{a_k + b_k}{2}, c_k \text{ is between } a_k \text{ and } b_k \quad (4)$$

Step 3: If $|x_{n+1} - x_n| < \epsilon, |f(x_n)| < \epsilon, \epsilon = 10^{-9}$ as a tolerance; stop else go to Step 2.

5. Results and Discussion

Two numerical iterations is suggested to introduce the performance of the Illinois Algorithm (IRFM) represented in Eq. 3 acquired in the present paper in order to solve non-linear equation with the initial value $x_0 = 1$ and we compare it with Two-Point Bracketing Method (TPBM) represented in Eq. 4 with two initial values x_0 and x_1 . For convergence criteria, the distance between two consecutive iterates is based on Eq. 5, less than 10^{-9} . Five examples in Eq. 2 are used for numerical testing with the R values from 1-5 ohm, represents (load resistance) of the circuit. All determinations are carried out with the algorithm precision introduced in Tables and Figures 1 to 5 and the number of function evaluations needed are extracted from the Eq. 2. The numerical examples and the approximate solutions produced by two techniques for solving Eq. 2.

The following Tables and Figs. indicate that TPBM algorithm needs 5 iterations while IRFM technique need 6 iterations to reach to the convergence which proves that TPBM is faster than IRFM.

Table 1 - From Iterative techniques IRFM and TPBM.

Iterations	V_{pv} -IRFM	I_{pv} -IRFM	P_{pv} -IRFM	V_{pv} -TPBM	I_{pv} -TPBM	P_{pv} -TPBM	ϵ -IRFM	ϵ -TPBM
1	0.942216008	0.942216008	0.88777101	0.934955239	0.934955239	0.874141299	0.019792873	0.012532104
2	0.927694471	0.927694471	0.86061703	0.925298174	0.925298174	0.856176710	0.005271336	0.002875039
3	0.922901876	0.922901876	0.85174787	0.922665275	0.922665275	0.851311210	0.000478742	0.00024214
4	0.922428674	0.922428674	0.85087466	0.922425905	0.922425905	0.850869550	5.5397E-06	2.76985E-06
5	0.922423135	0.922423135	0.85086444	0.922423135	0.922423135	0.850864440	9.515E-10	0
6	0.922423135	0.922423135	0.85086444				0	

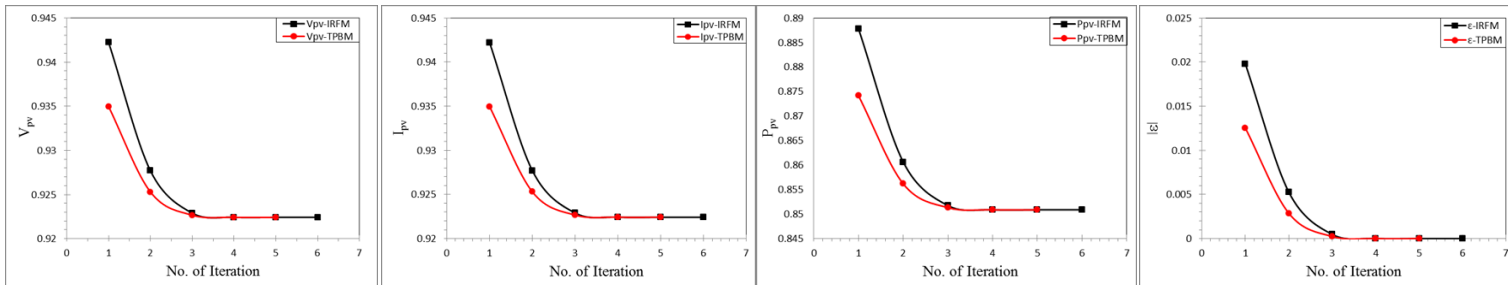


Fig. 1 - Results from IRFM and TPBM techniques.

Table 2 - From Iterative techniques IRFM and TPBM.

Iterations	V_{pv} -IRFM	I_{pv} -IRFM	P_{pv} -IRFM	V_{pv} -TPBM	I_{pv} -TPBM	P_{pv} -TPBM	ϵ -IRFM	ϵ -TPBM
1	0.940570850	0.470285425	0.442336762	0.932387877	0.466193938	0.434673576	0.023535468	0.015352490
2	0.924204903	0.462102452	0.427077352	0.921043240	0.460521620	0.424160325	0.007169521	0.004007854
3	0.917881577	0.458940788	0.421253294	0.917466619	0.458733309	0.420872498	0.000846194	0.000431232
4	0.917051661	0.458525830	0.420491874	0.917043526	0.458521763	0.420484414	1.62783E-05	8.13915E-06
5	0.917035390	0.458517695	0.420476954	0.917035386	0.458517693	0.420476950	8.06498E-09	0
6	0.917035382	0.458517691	0.420476946				1.88738E-15	
7	0.917035382	0.458517691	0.420476946				0	

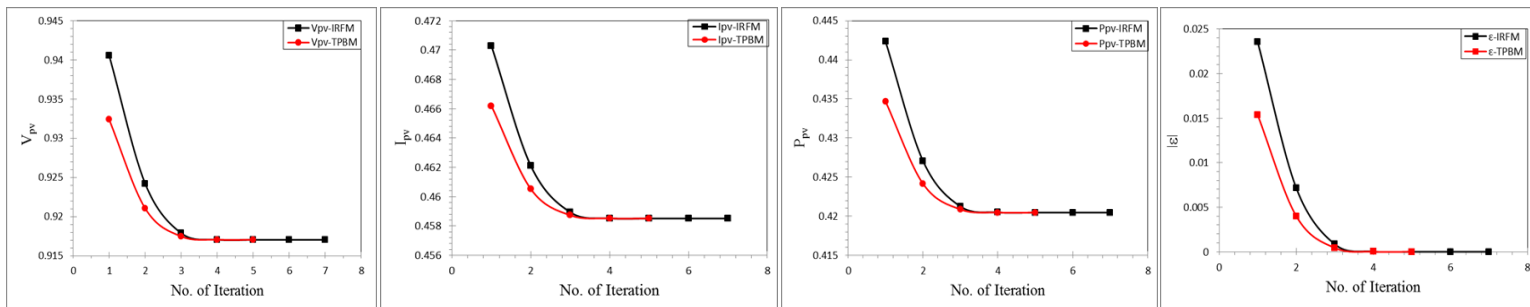


Fig. 2 – Results from IRFM and TPBM techniques.

Table 3 - From Iterative techniques IRFM and TPBM.

Iterations	V_{pv} -IRFM	I_{pv} - IRFM	P_{pv} -IRFM	V_{pv} -TPBM	I_{pv} -TPBM	P_{pv} -TPBM	ϵ -IRFM	ϵ -TPBM
1	0.938877255	0.312959085	0.293830166	0.929642988	0.309880996	0.288078695	0.028473881	0.019239614
2	0.920408721	0.306802907	0.282384071	0.916189290	0.305396430	0.279800938	0.010005347	0.005785916
3	0.911969859	0.303989953	0.277229674	0.911212525	0.303737508	0.276769422	0.001566485	0.000809151
4	0.910455191	0.303485064	0.276309552	0.910429322	0.303476441	0.276293850	5.18173E-05	2.59481E-05
5	0.910403453	0.303467818	0.276278149	0.910403413	0.303467804	0.276278125	7.88982E-08	3.94491E-08
6	0.910403374	0.303467791	0.276278101	0.910403374	0.303467791	0.276278101	2.03726E-13	0
7	0.910403374	0.303467791	0.276278101				0	

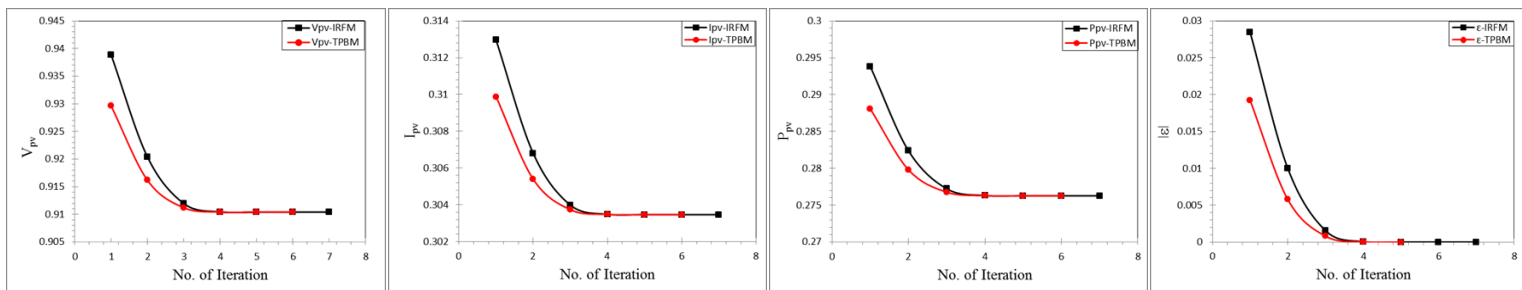


Fig. 3 – Results from IRFM and TPBM techniques.

Table 4 - From Iterative techniques IRFM and TPBM.

Iterations	V_{pv} -IRFM	I_{pv} - IRFM	P_{pv} -IRFM	V_{pv} -TPBM	I_{pv} -TPBM	P_{pv} -TPBM	ϵ -IRFM	ϵ -TPBM
1	0.937133368	0.234283342	0.219554737	0.926698007	0.231674502	0.214692299	0.035392766	0.024957405
2	0.916262647	0.229065662	0.209884309	0.910554356	0.227638589	0.207277309	0.014522045	0.008813754
3	0.904846066	0.226211516	0.204686601	0.903386681	0.225846670	0.204026874	0.003105464	0.001646079
4	0.901927296	0.225481824	0.203368212	0.901834428	0.225458607	0.203326334	0.000186694	9.38262E-05
5	0.901741560	0.225435390	0.203284460	0.901741081	0.225435270	0.203284244	9.5847E-07	4.79235E-07
6	0.901740602	0.225435151	0.203284028	0.901740602	0.225435151	0.203284028	3.03469E-11	0
7	0.901740602	0.225435150	0.203284028				0	

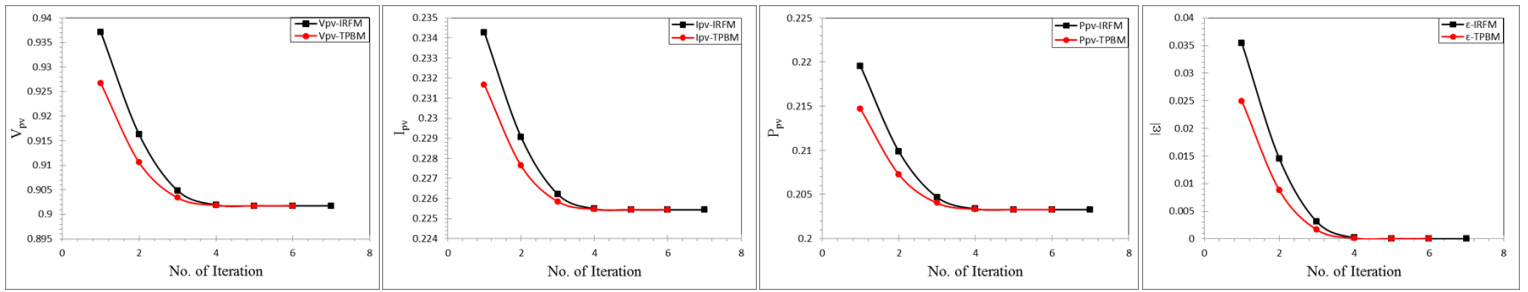


Fig. 4 – Results from IRFM and TPBM techniques.

Table 5 - From Iterative techniques IRFM and TPBM.

Iterations	V_{pv} -IRFM	I_{pv} -IRFM	P_{pv} -IRFM	V_{pv} -TPBM	I_{pv} -TPBM	P_{pv} -TPBM	ϵ -IRFM	ϵ -TPBM
1	0.935337263	0.187067453	0.174971159	0.923526458	0.184705292	0.170580224	0.046244548	0.034433744
2	0.911715654	0.182343131	0.166245087	0.903865572	0.180773114	0.163394594	0.022622939	0.014772857
3	0.896015489	0.179203098	0.160568751	0.892973327	0.178594665	0.159480273	0.006922775	0.003880613
4	0.889931165	0.177986233	0.158395496	0.889520496	0.177904099	0.158249343	0.000838451	0.000427782
5	0.889109827	0.177821965	0.158103257	0.889101276	0.177820255	0.158100216	1.71125E-05	8.56105E-06
6	0.889092724	0.177818545	0.158097174	0.889092720	0.177818544	0.158097173	9.60373E-09	4.80187E-09
7	0.889092715	0.177818543	0.158097171	0.889092715	0.177818543	0.158097171	3.10862E-15	0
8	0.889092715	0.177818543	0.158097171				0	

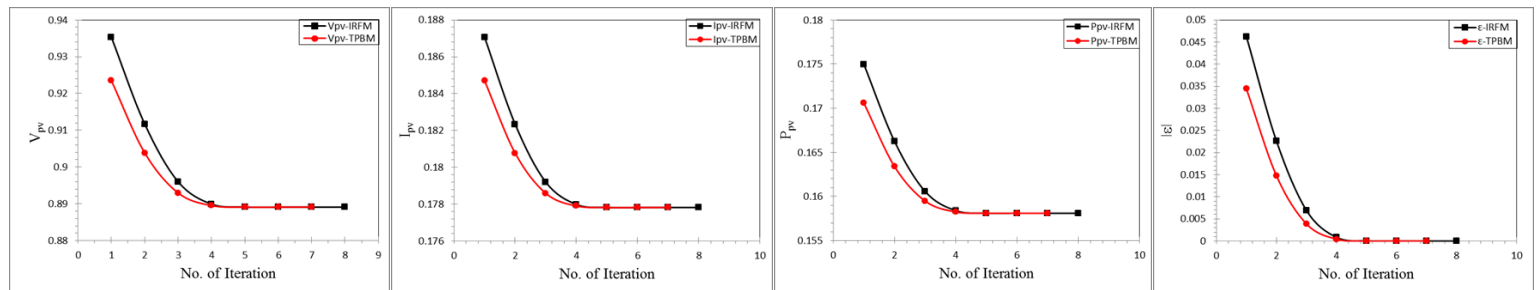


Fig. 5 – Results from IRFM and TPBM techniques.

6. Conclusion

The obtained results from the proposed method is comparable with the other methods Newton's and Two-Point Bracketing algorithms have been noticed in all cases in this paper. Several problems prove that the new proposed method is more accurate, efficient and easy to use with lesser iterations compared with other methods and realizes better than common and classical Newton's algorithm.

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